

# Simulating the structural diversity of astrophysical carbon clusters

Cyril Falvo

*Institut des Sciences Moléculaires d'Orsay  
Université Paris Sud – Université Paris Saclay  
Laboratoire Interdisciplinaire de Physique  
Université Grenoble Alpes*

- Institut des Sciences Moléculaires d'Orsay — Université Paris Sud
  - Maëlle Bonnin
  - Pascal Parneix
  - Thomas Pino
- Laboratoire Interdisciplinaire de Physique — Université Grenoble Alpes
  - Florent Calvo

# Carbon clusters: an astrophysical issue

- ~200 molecules have been detected in the Interstellar medium (ISM)



Horsehead nebula

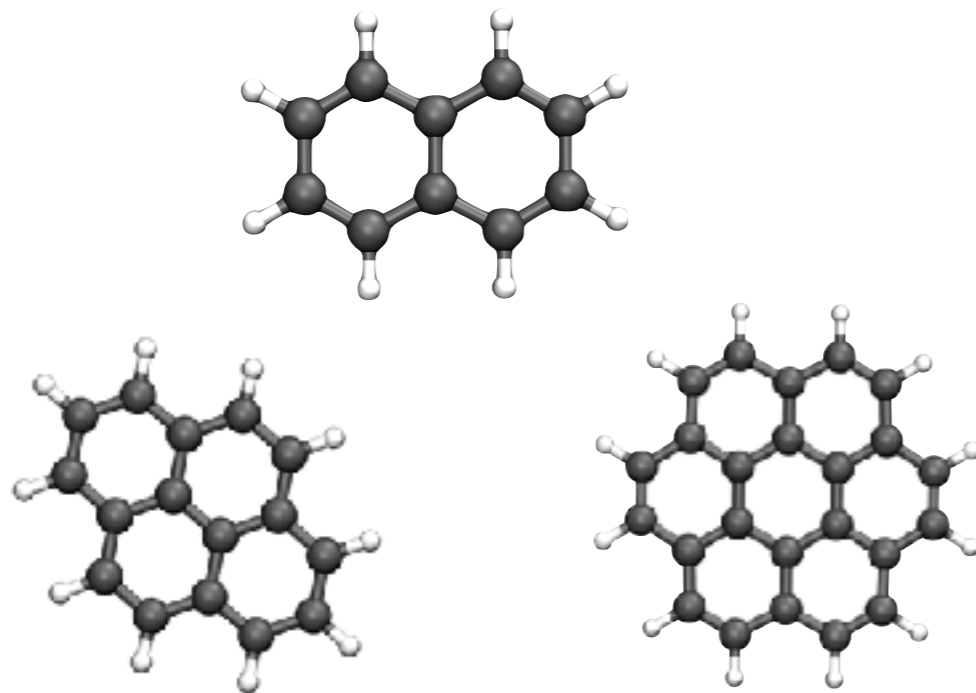


Iris nebula

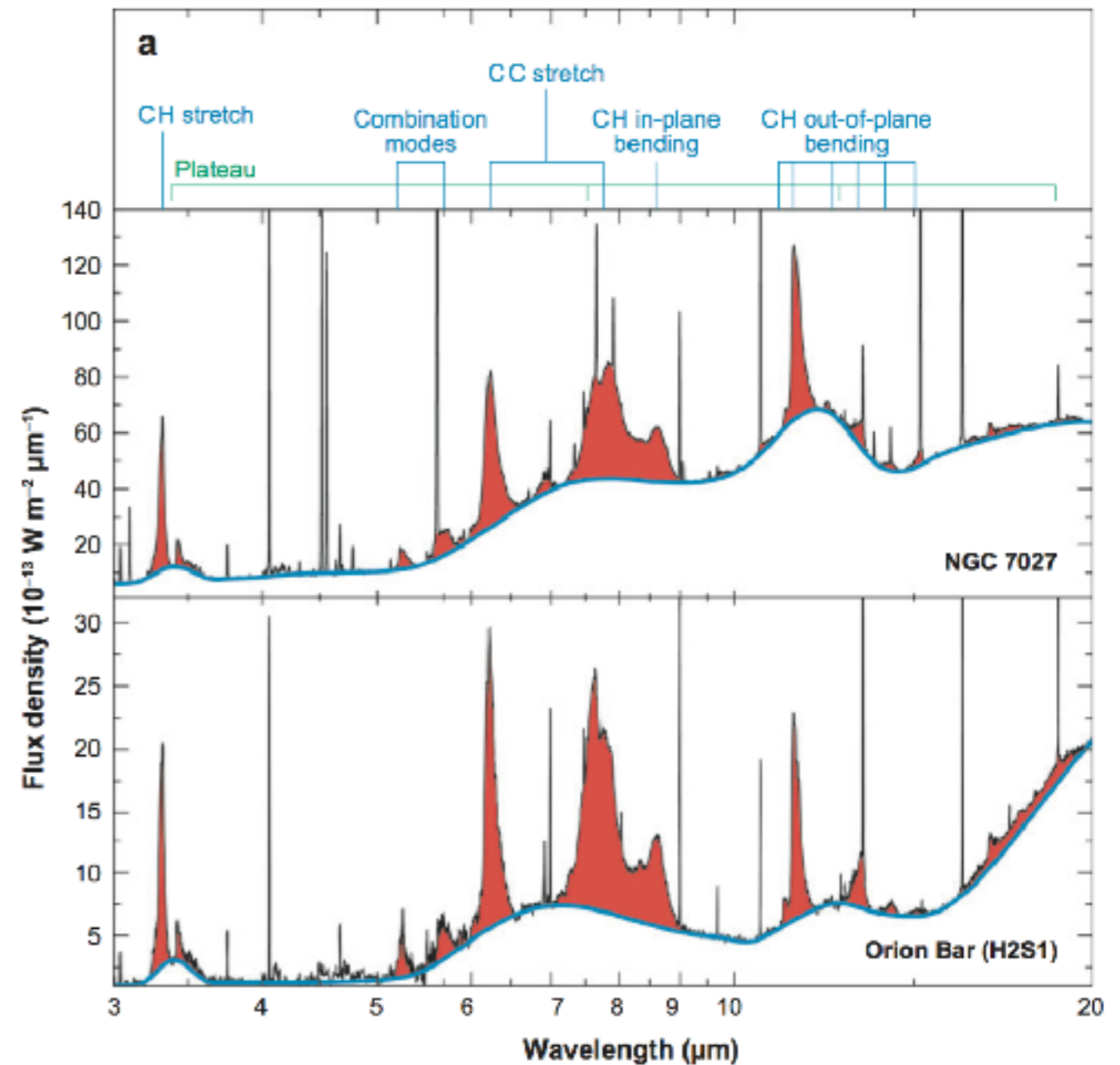
- The ISM is composed of H, He, C, O, N, ...

# Carbon clusters: an astrophysical issue

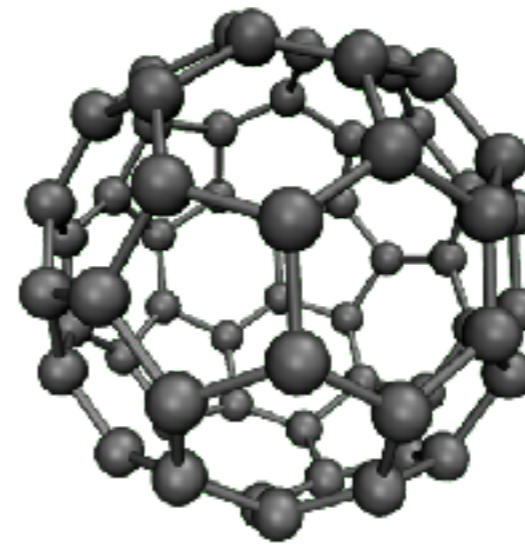
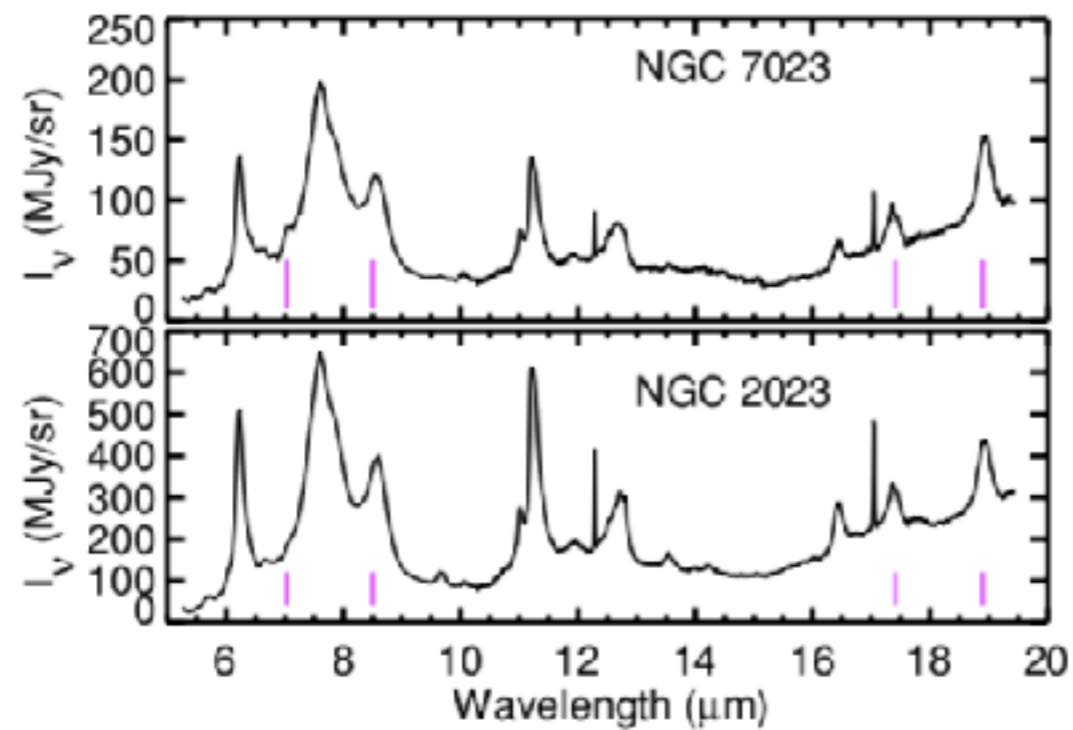
- The presence of polycyclic aromatic hydrocarbons (PAH) in the ISM have been suggested for more than 30 years.
- No clear identification of a specific PAH have been achieved



Tielens, Annu. Rev. Astron. Astrophys. 46, 289 (2008)

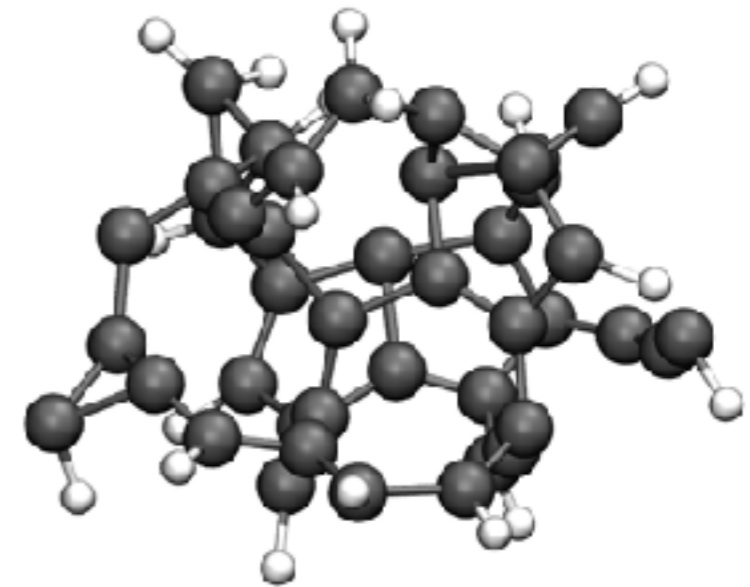
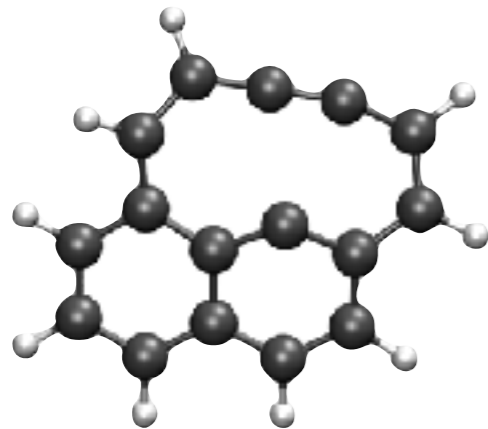
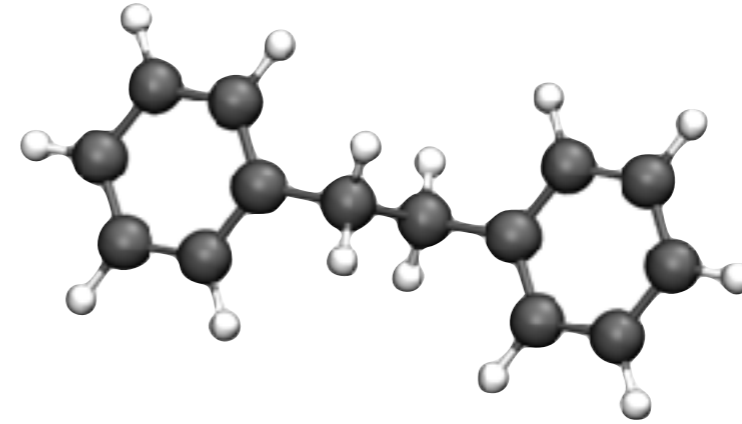
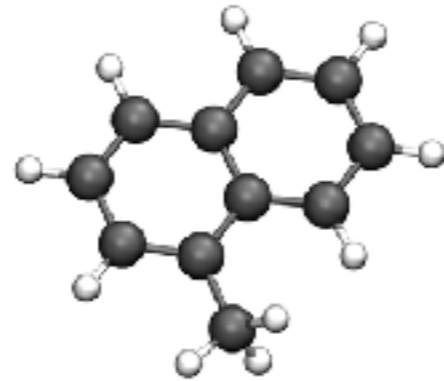
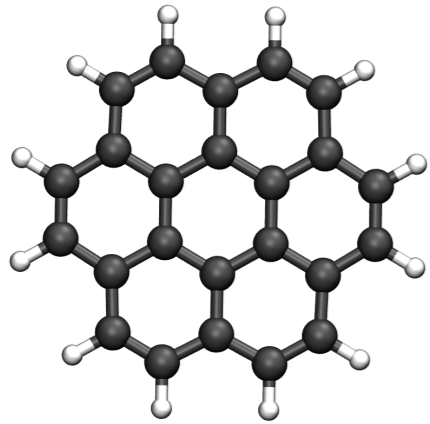


- C<sub>60</sub> Buckminsterfullerene have been identified in 2010 in the ISM



*Sellgren et al. Astrophys. J. Lett. 722, L54 (2010)*

# Polycyclic Aromatic Aliphatic Mixed Hydrocarbons



- Explore the diversity of hydrocarbon structures without preconceived model through the use of atomistic simulations
- Compute the spectroscopic response (IR and UV/Visible) of these structures
- Link structure to spectroscopic response in order to obtain more information from observational data

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We start with carbon clusters  $C_{24}$ ,  $C_{42}$ , and  $C_{60}$





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⚠ REBO and AIREBO have suffered and still suffer from several issues in LAMMPS

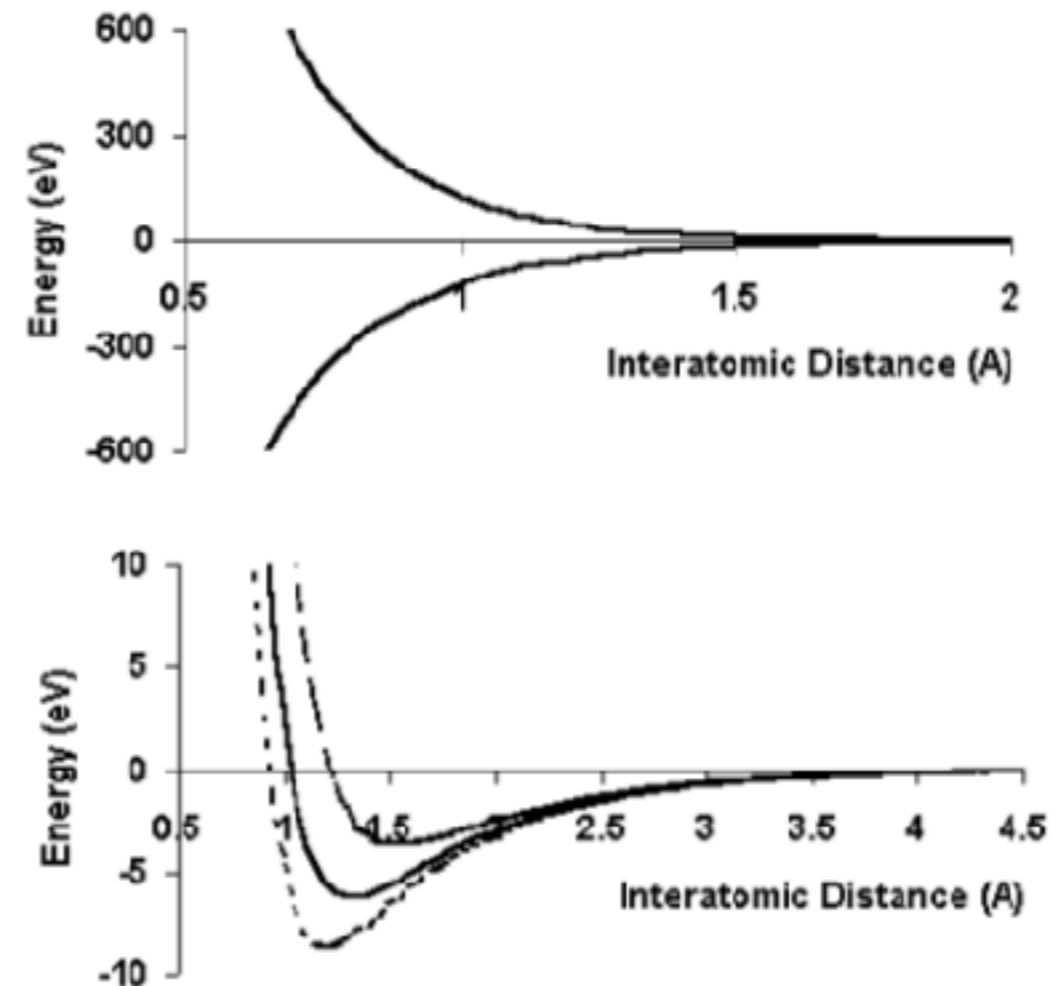


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$$V = \sum_{i < j} (V^R(r_{ij}) - b_{ij} V^A(r_{ij}))$$

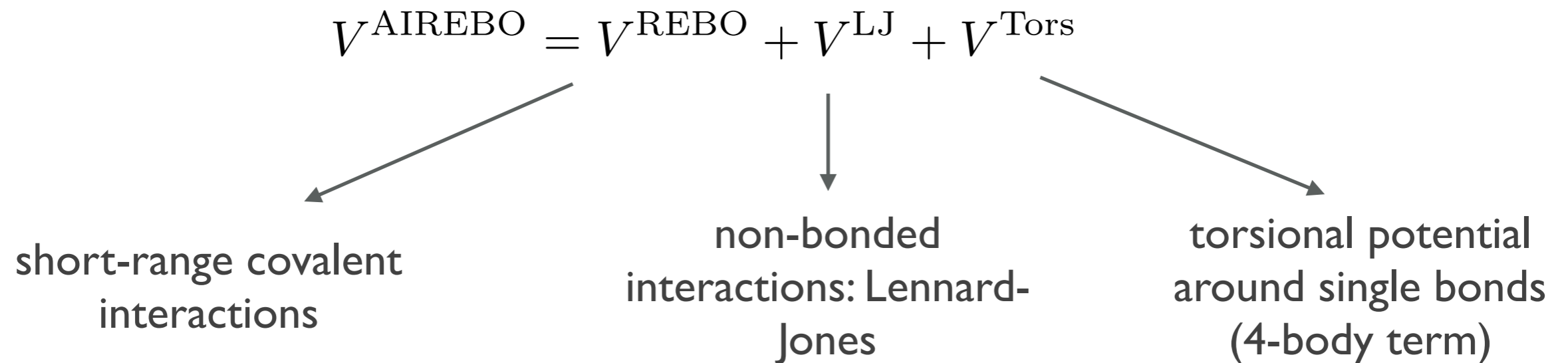
- $b_{ij}$ : function of the environment of the bond. Includes 3-body and 4-body terms



**Figure 1.** Plots of the pair potentials (5) and (6) obtained using the parameters in table 1. Top: attractive and repulsive pair terms as a function of interatomic distance. Bottom: pair potentials for triple bonds (dotted curve), double bonds (solid curve), and single bonds (dashed curve) obtained by multiplying the attractive pair term by the appropriate bond order value and adding the repulsive pair term.

*Brenner et al. J. Phys. Cond. Mat., 14, 783 (2002)*

- AIREBO potential introduced in 2000 by Stuart *Stuart et al., JCP **112** 6472 (2000)*



- It has been known for several years that (AI)REBO implemented in LAMMPS suffered from bugs

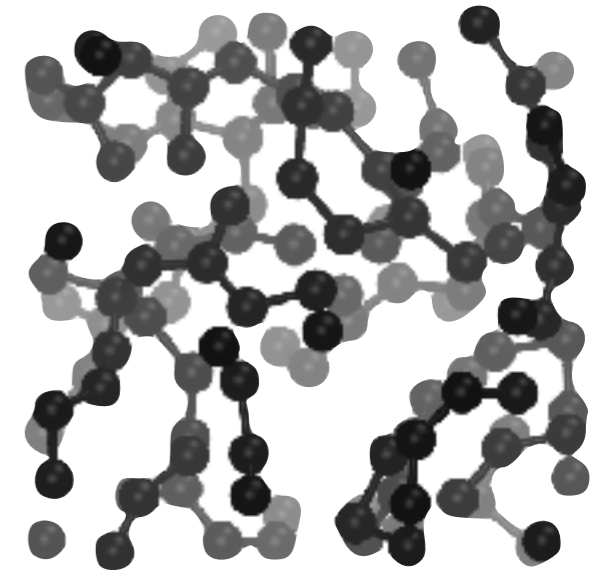
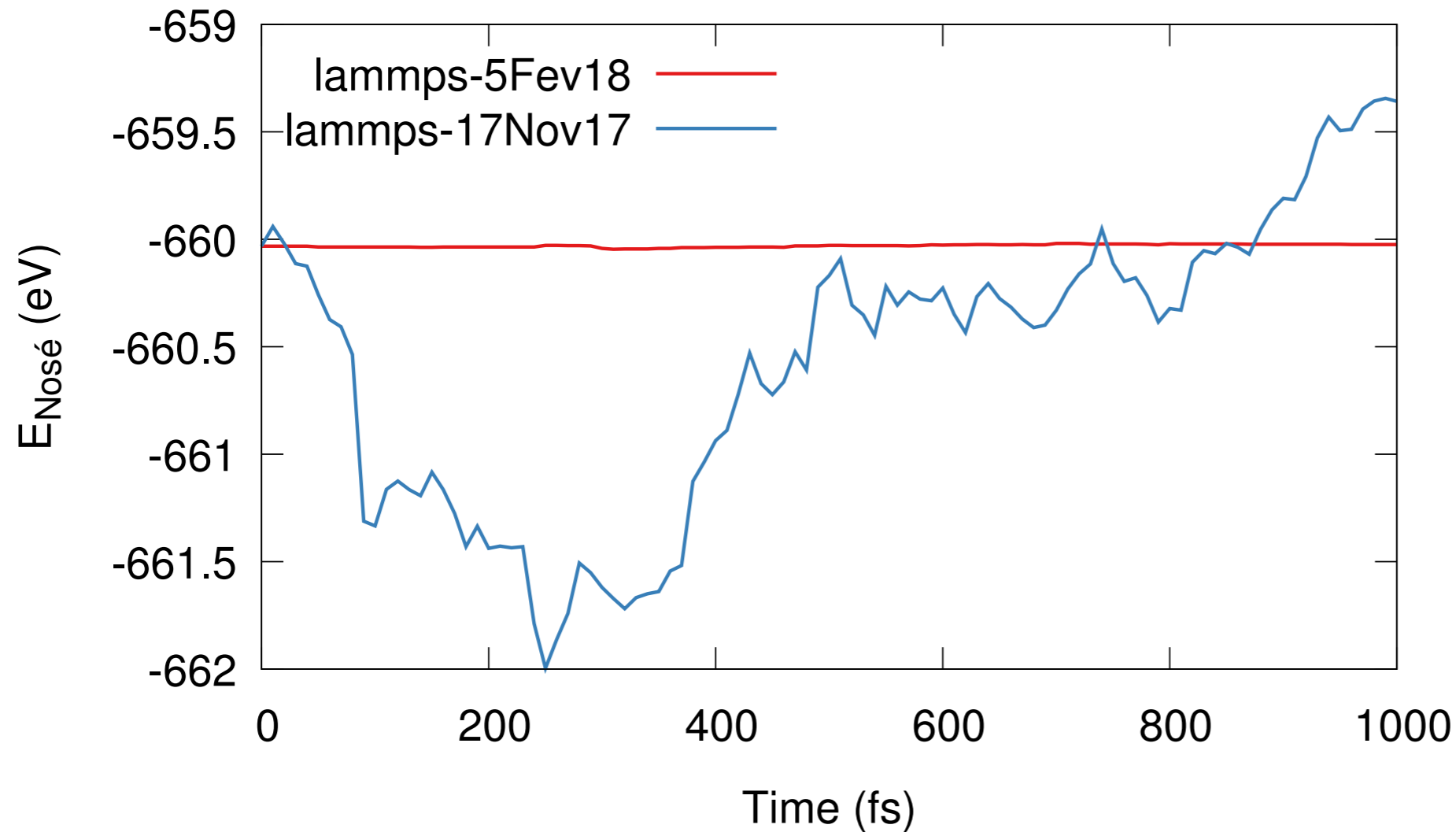
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- Several LAMMPS users/developers contributed to fix several bugs in the force calculation of the (AI)REBO potentials
- With the Aug. 2017 release of LAMMPS these bugs were corrected
  - spline coefficients read from an input file did not correspond to hard-coded parameters
  - AIREBO in LAMMPS was implemented from a transcription of a Fortran code which included a bug in the force calculation (LJ part).

# Benchmark: liquid carbon

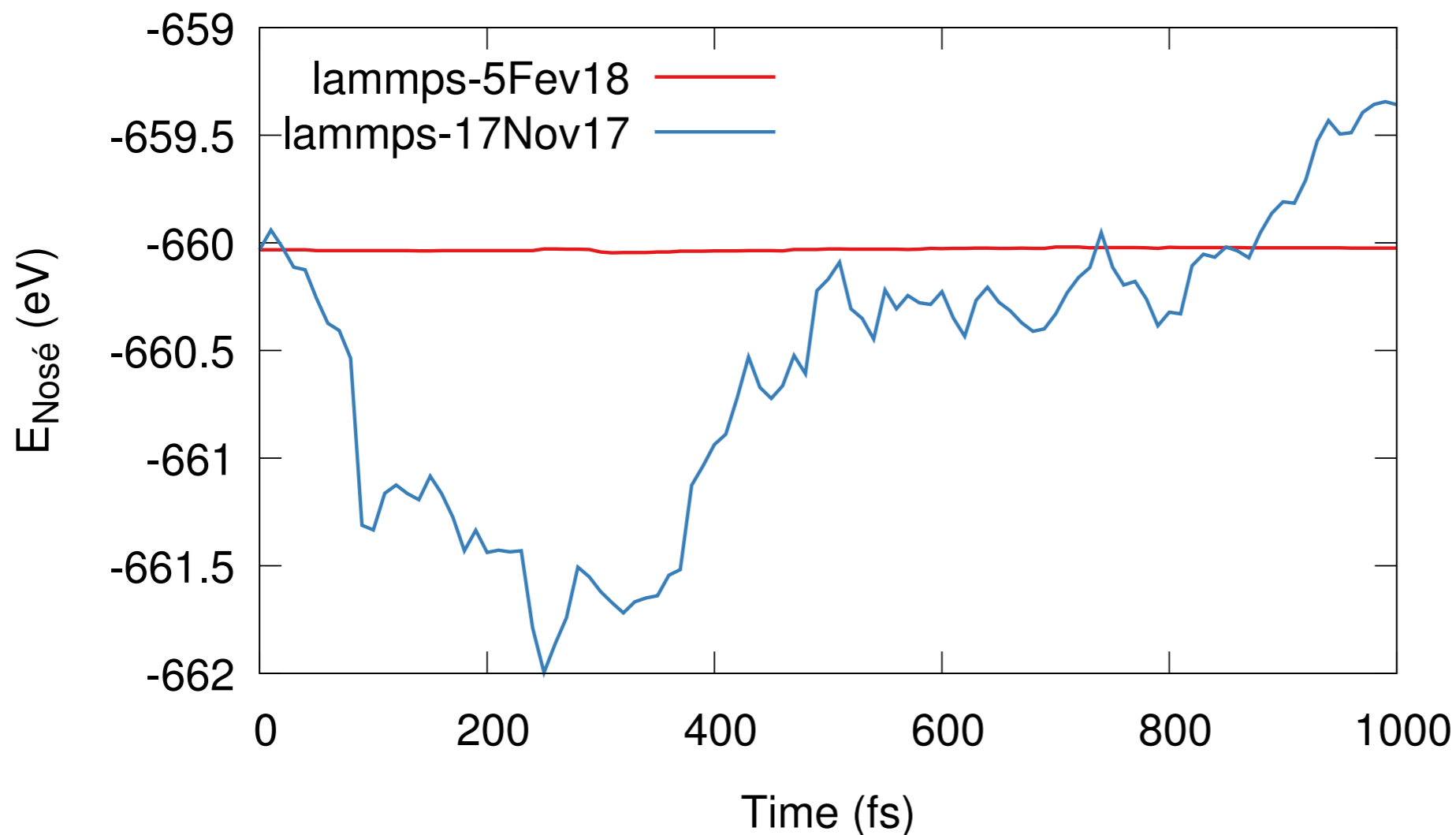
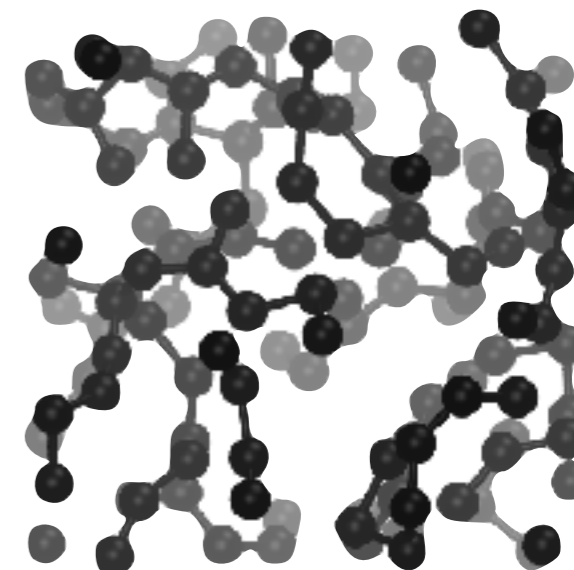
- Box of 128 carbon atoms at 5000 K with PBC (NVT)  
 $\rho=2 \text{ g.cm}^{-3}$ ,  $\Delta t=0.01 \text{ fs}$





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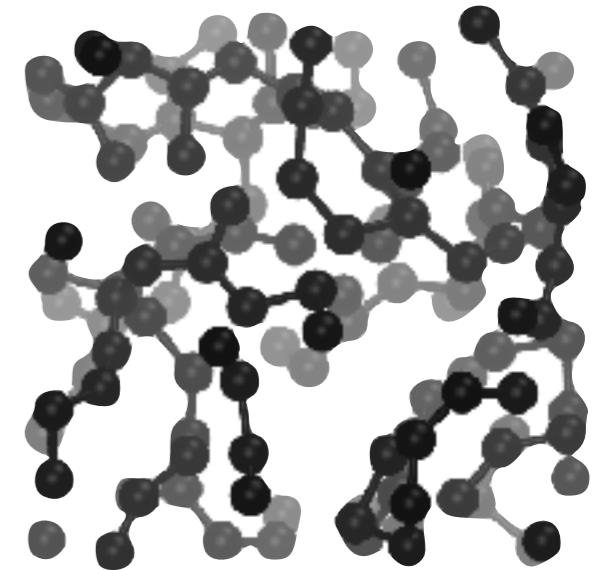
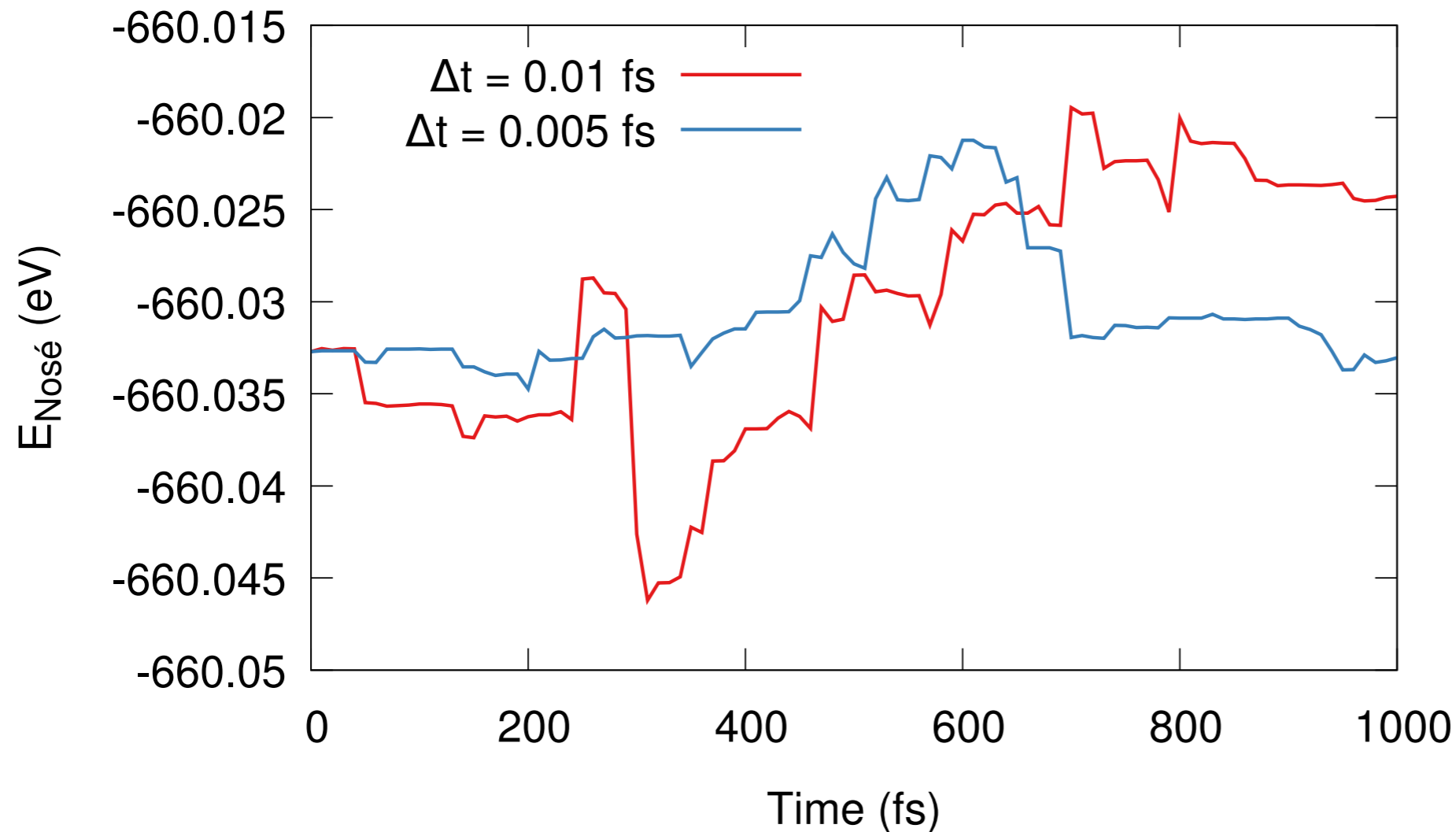
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Can we now safely use AIREBO with LAMMPS ?

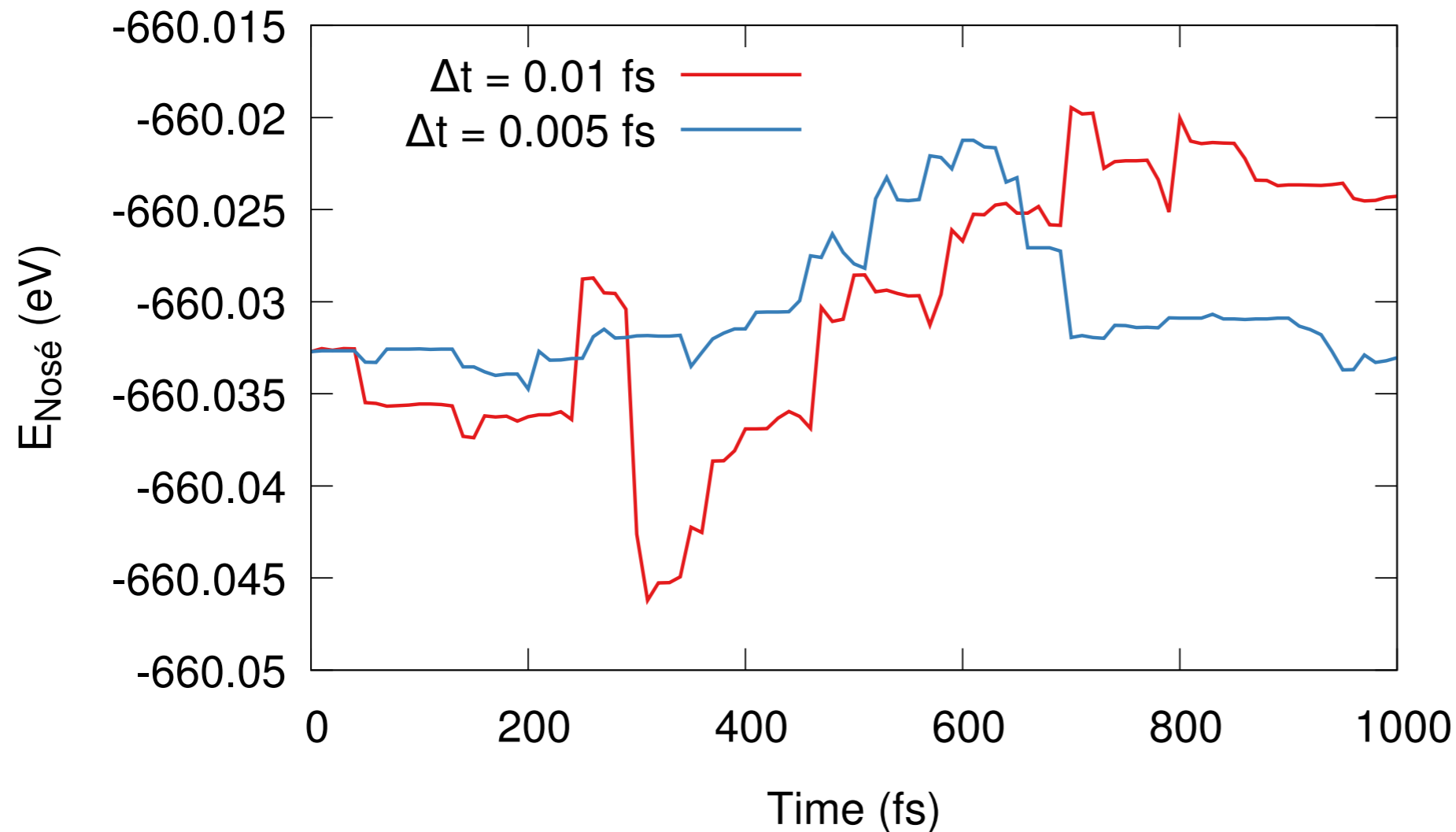
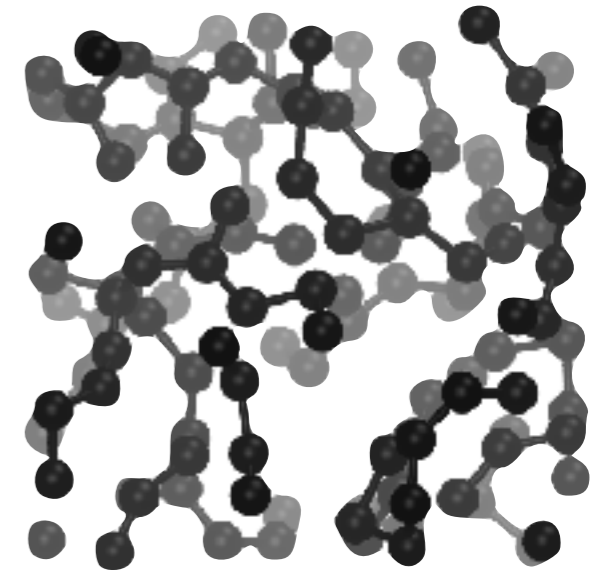
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Energy jumps remain even at very small timesteps

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$$C_{ij} = 1 - \max \{ w_{ij}(r_{ij}), w_{ik}(r_{ik})w_{kj}(r_{kj}) \quad \forall k, w_{ik}(r_{ik})w_{kl}(r_{kl})w_{lj}(r_{lj}) \quad \forall k, l \}$$

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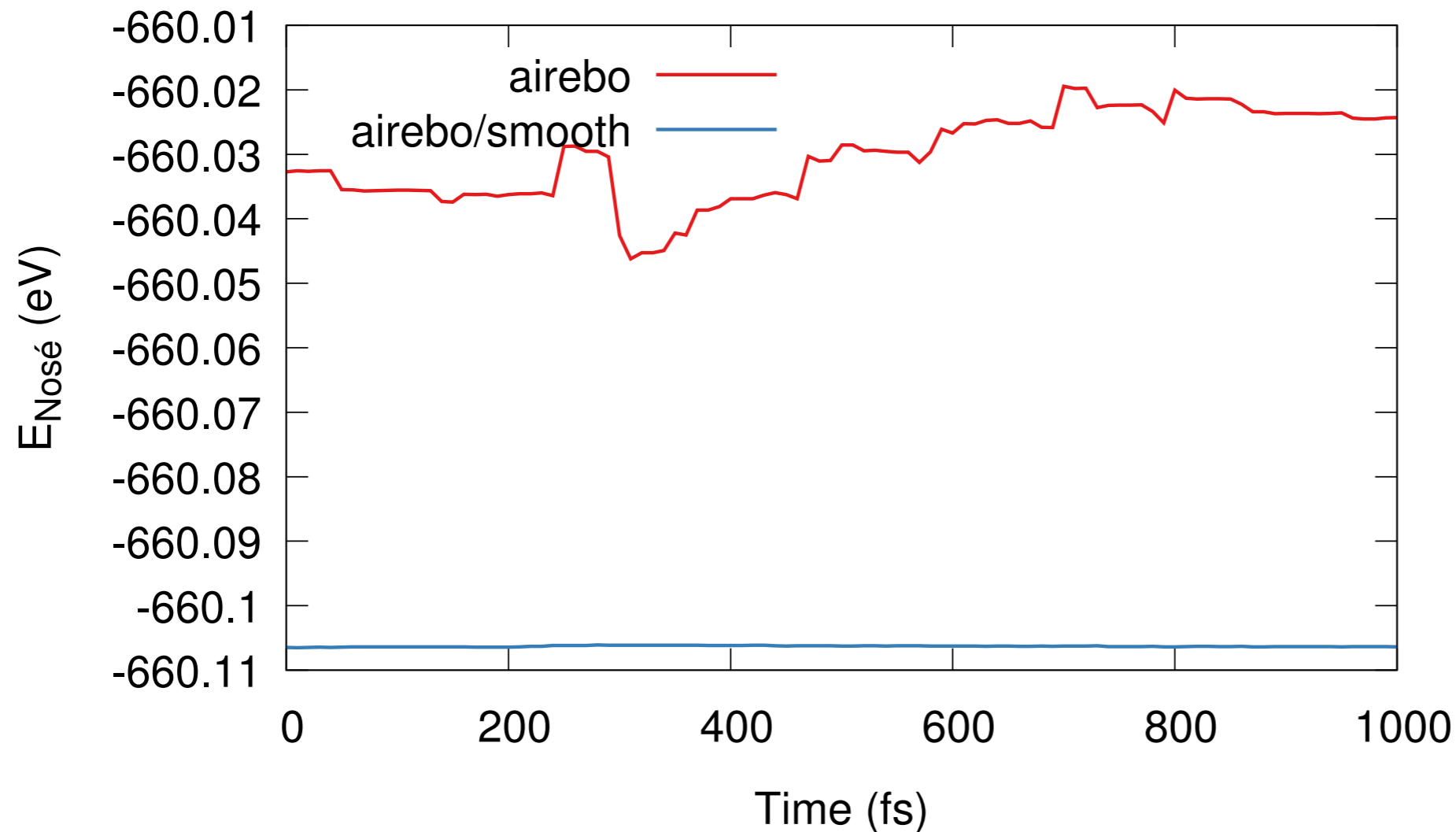
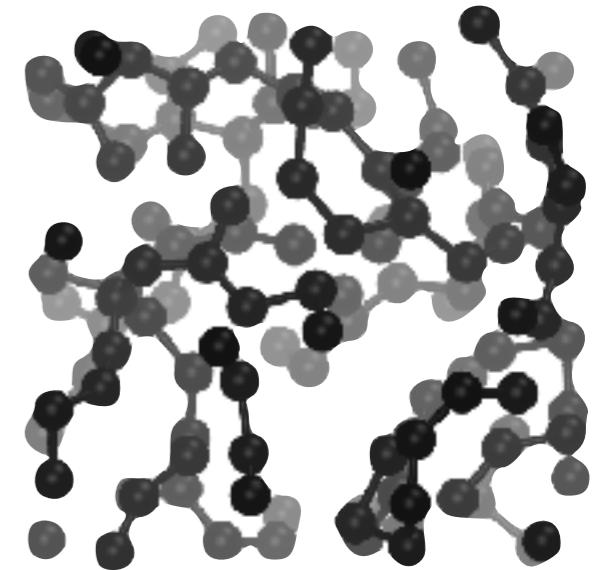
- Smooth version of the connectivity switch

$$C_{ij} = (1 - w_{ij}) \prod_{k \neq i, j} (1 - w_{ik}w_{kj}) \prod_{k, l \neq i, j} (1 - w_{ik}w_{kl}w_{lj})$$

⚠ this function has not been properly tested

# Benchmark: liquid carbon

- Box of 128 carbon atoms at 5000 K with PBC (NVT)  
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Energy conservation is finally recovered !



Can we safely use AIREBO with LAMMPS ?

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Can we safely use AIREBO ?

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	Brenner 2002	REBO	REBO'
Ethylene	-24.4077	-24.5284	-24.4077
Cyclopropene	-28.2589	-28.3610	-28.2589
Allene	-30.2392	-30.3511	-30.2392
Propene	-37.3047	-37.5116	-37.3047
Cyclobutene	-42.1801	-42.3536	-42.1797
1,3-Butadiene	-43.0035	-43.3977	-43.0035
1-Butene	-50.0487	-50.2557	-50.0486
2-Butene	-50.2017	-50.4951	-50.2016
1,4-Pentadiene	-56.5078	-56.9220	-56.5079
Cyclopentene	-57.1119	-57.3895	-57.1121
2-Methyl-1-butene	-62.9658	-63.0254	-62.9658
2-Methyl-2-butene	-63.1109	-63.2642	-63.1188
Benzene	-59.3096	-60.2313	-59.3096
Naphthalene	-93.8784	-95.0955	-93.8785

REBO: potential given in distributed version of LAMMPS (02/2018)

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average error for REBO: 335 meV

average error for REBO': 2 meV

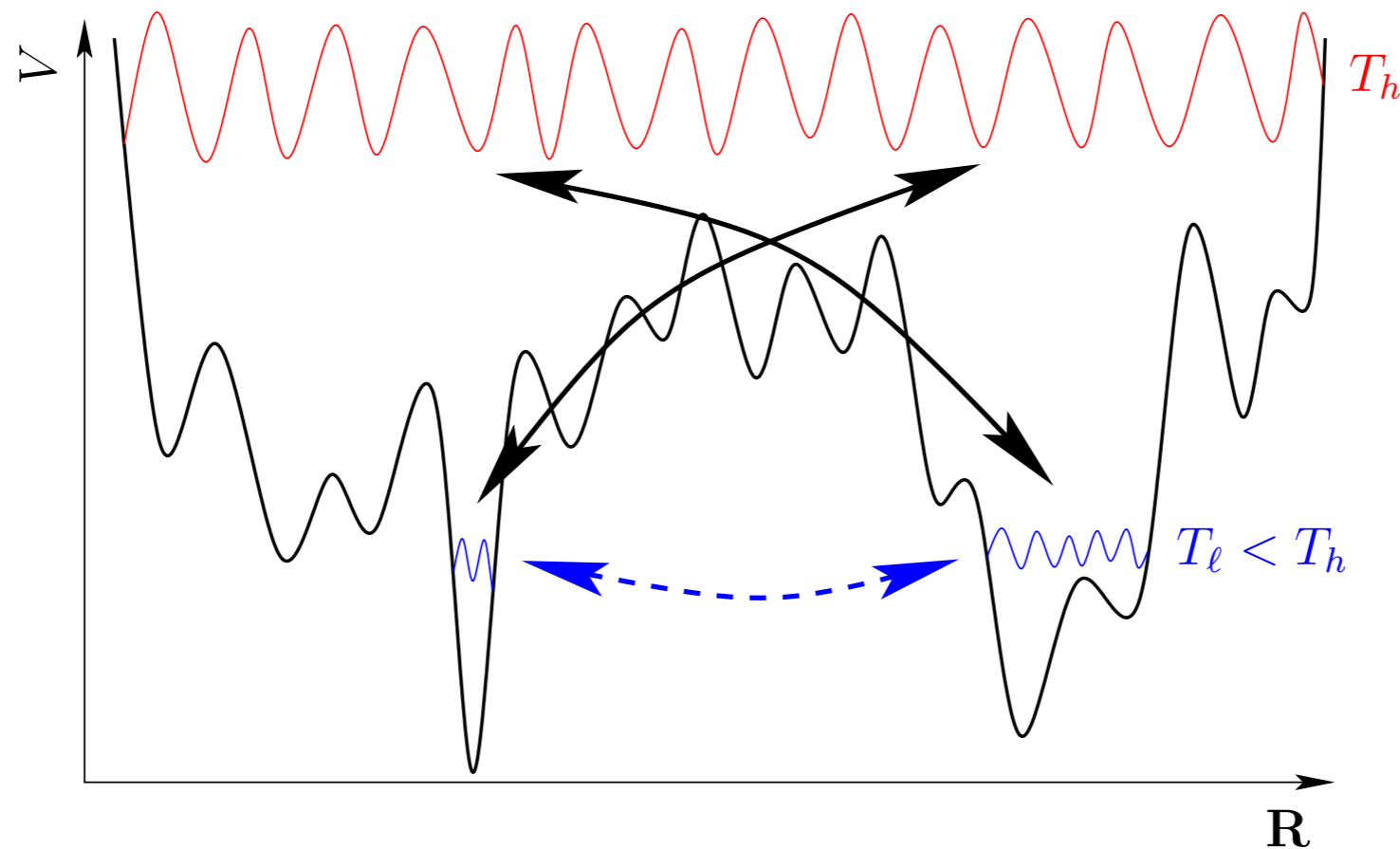


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## Use of Replica Exchange Molecular Dynamics (REMD) simulations







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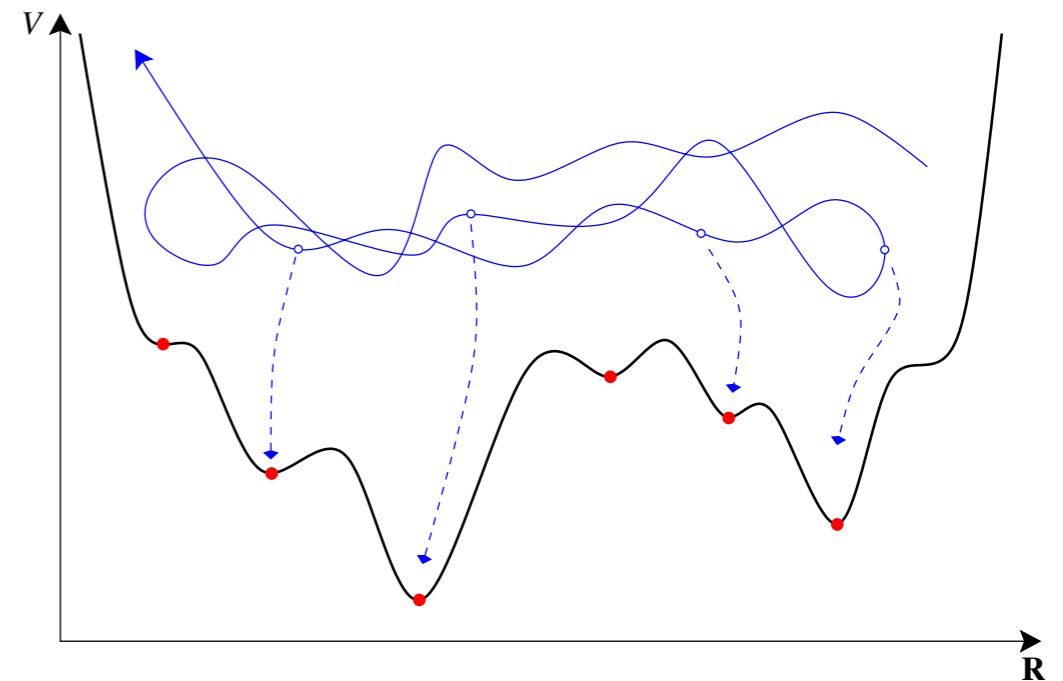
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Cluster	$T_{\min}$ (K)	$T_{\max}$ (K)	$N_{\text{temp}}$	$R_{\min}$ (Å)	$R_{\max}$ (Å)
$C_{24}$	1500	6500	12	4.1	16.6
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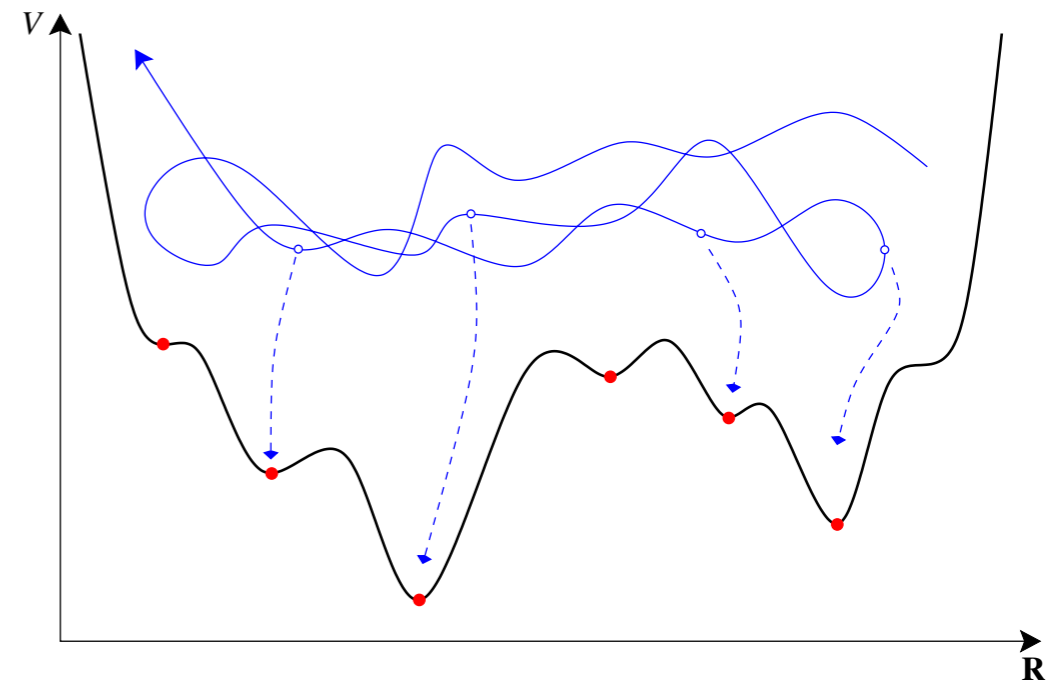
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- Elimination of redundant structures and dissociated structures



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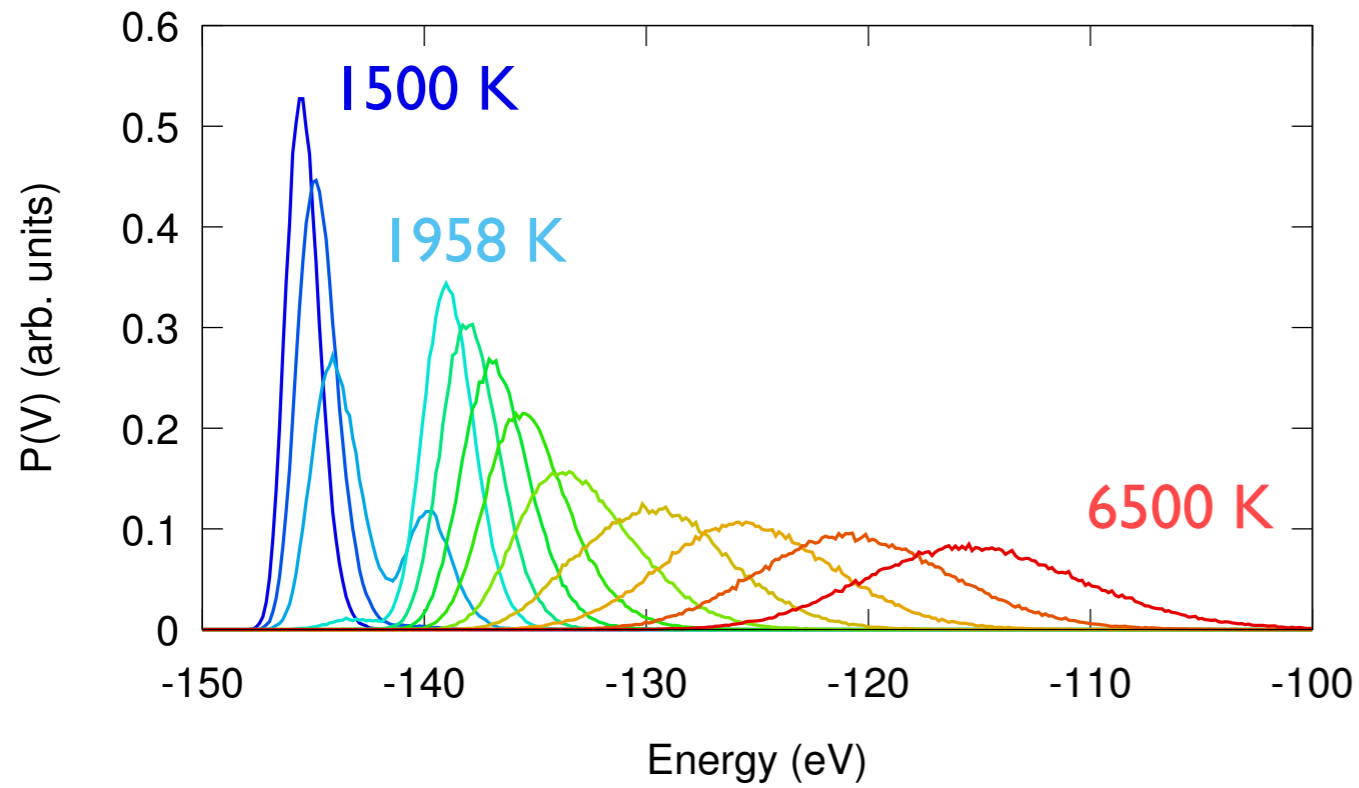
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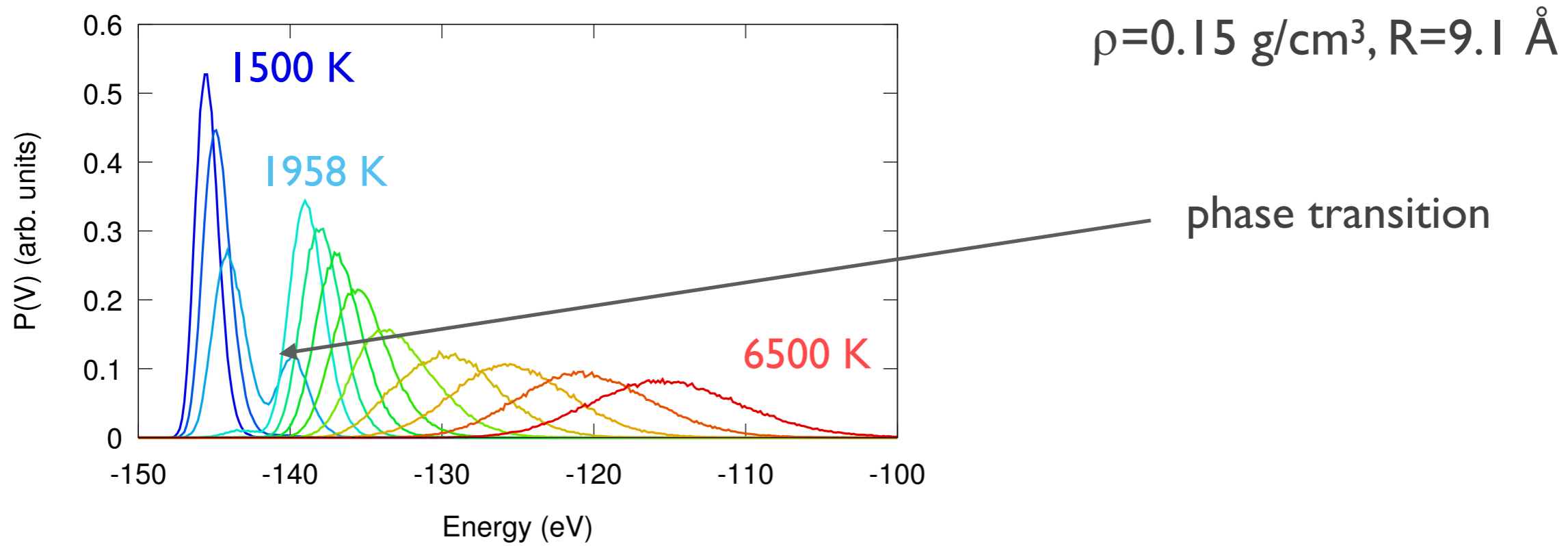
Cluster	before selection	dissociated	redundant	final
$C_{24}$	1,500,060	149,933	1,251,764	98,363
$C_{42}$	1,400,056	282,204	631,380	486,472
$C_{60}$	1,600,064	320,332	623,294	656,438

# C<sub>24</sub>: example of REMD simulation

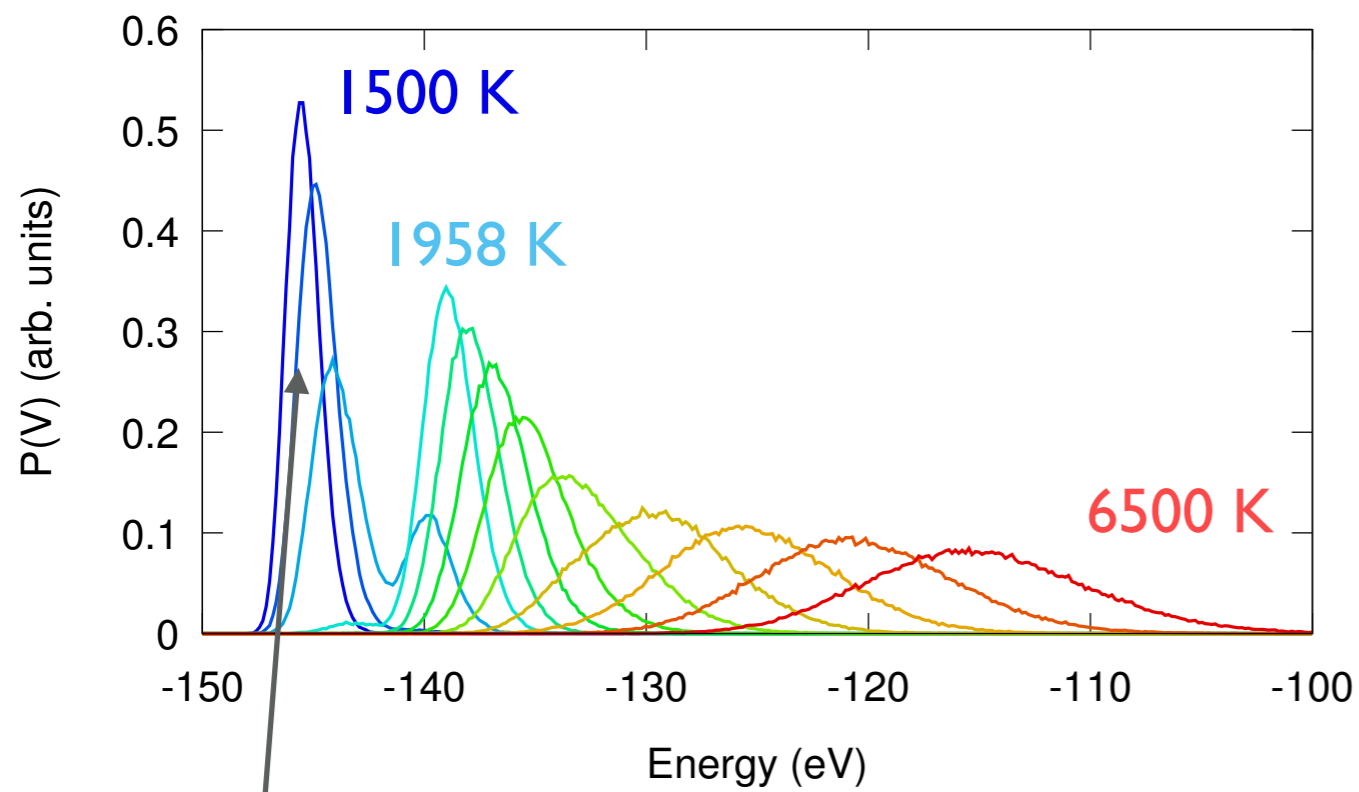


$\rho=0.15 \text{ g/cm}^3$ ,  $R=9.1 \text{ \AA}$

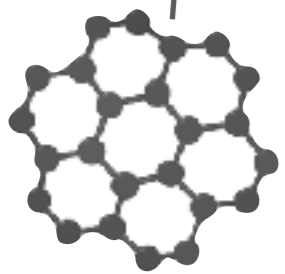
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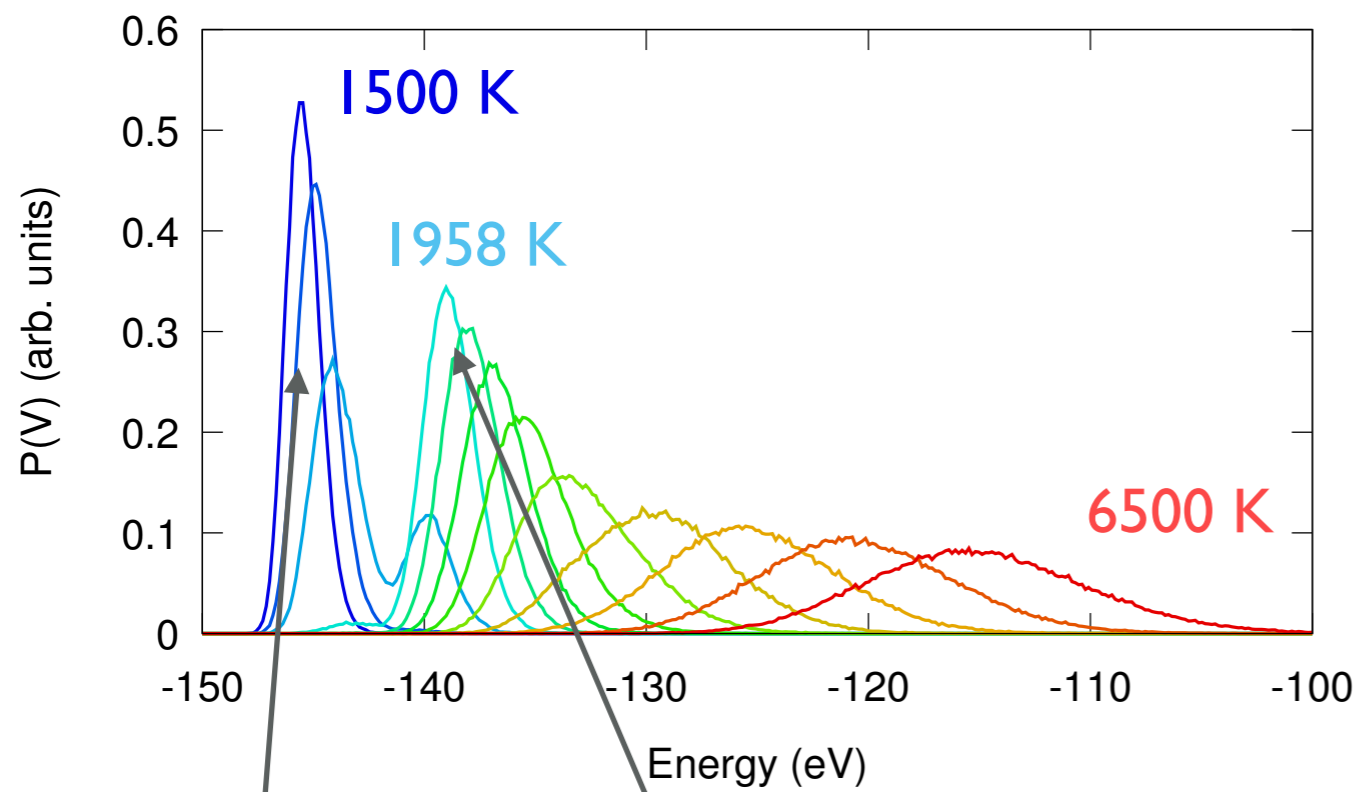
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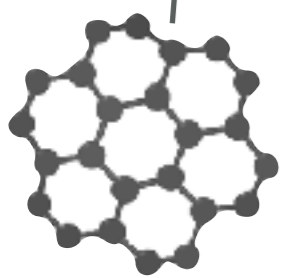
planar hexagonal



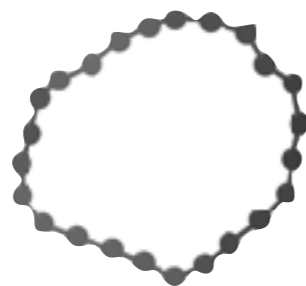
# C<sub>24</sub>: example of REMD simulation



$\rho=0.15 \text{ g/cm}^3$ ,  $R=9.1 \text{ \AA}$

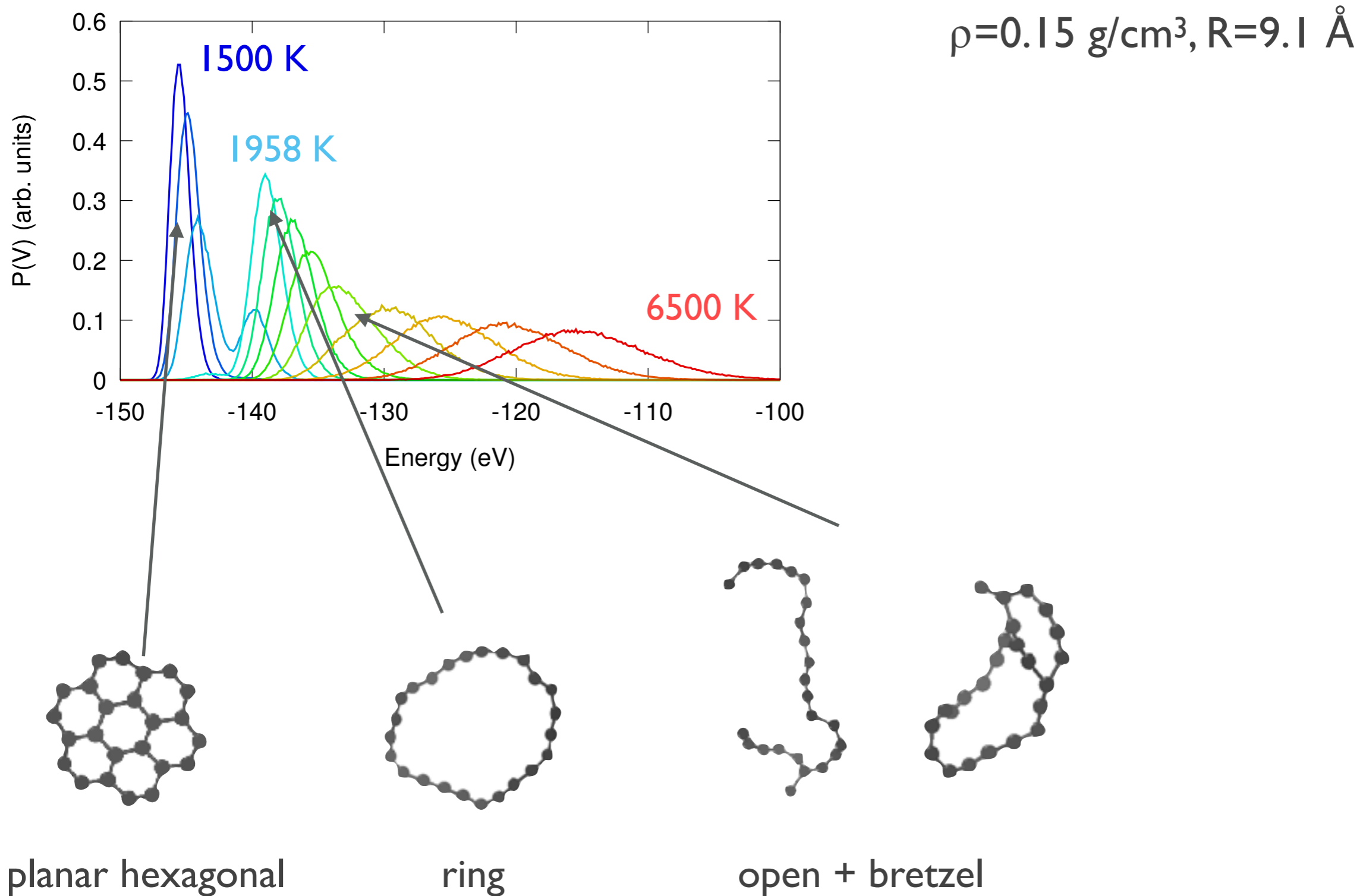


planar hexagonal

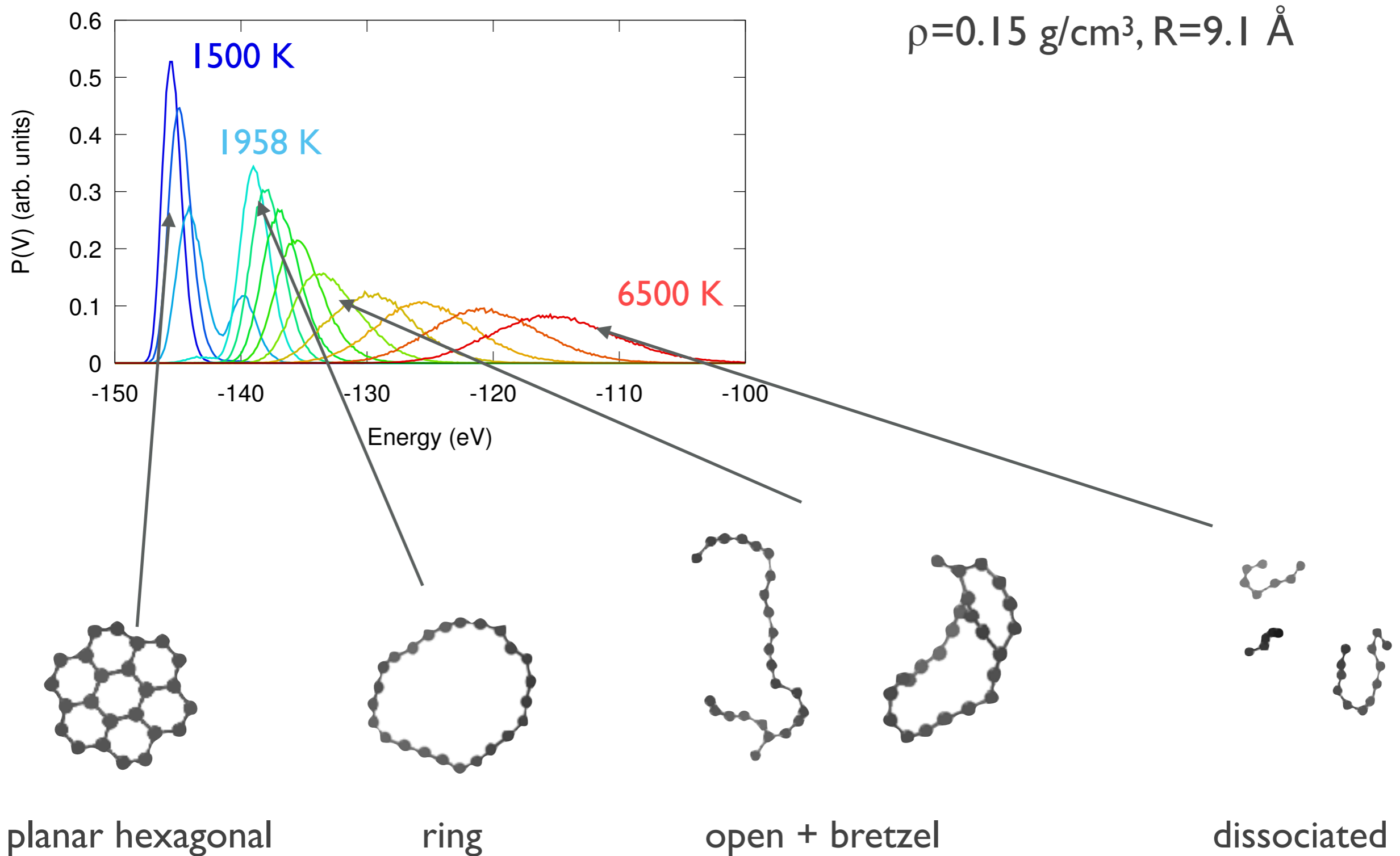


ring

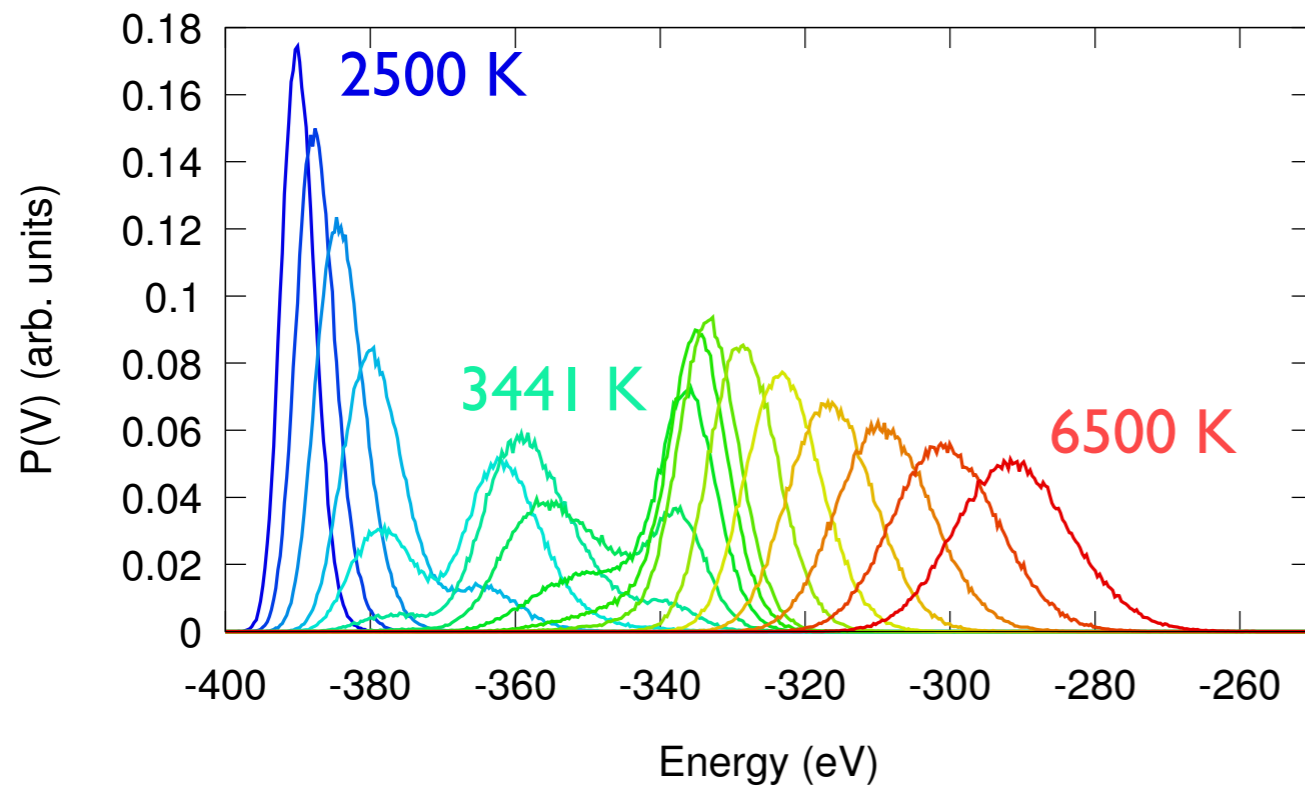
# C<sub>24</sub>: example of REMD simulation



# C<sub>24</sub>: example of REMD simulation

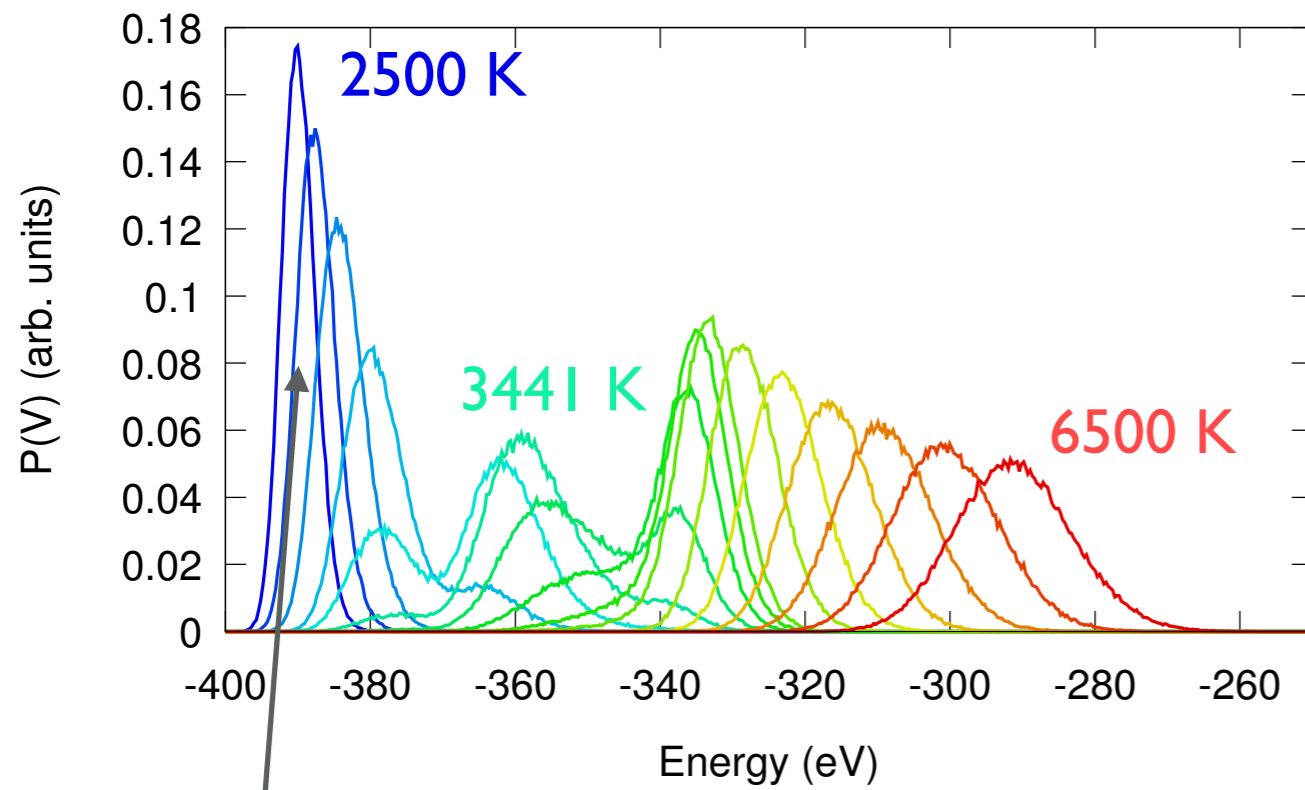


# C<sub>60</sub>: example of REMD simulation

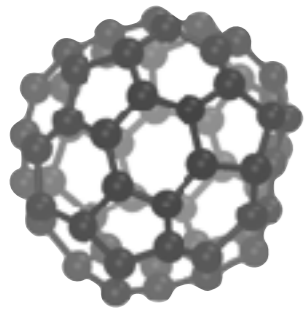


$\rho=0.15 \text{ g/cm}^3$ ,  $R=12.4 \text{ \AA}$

# C<sub>60</sub>: example of REMD simulation

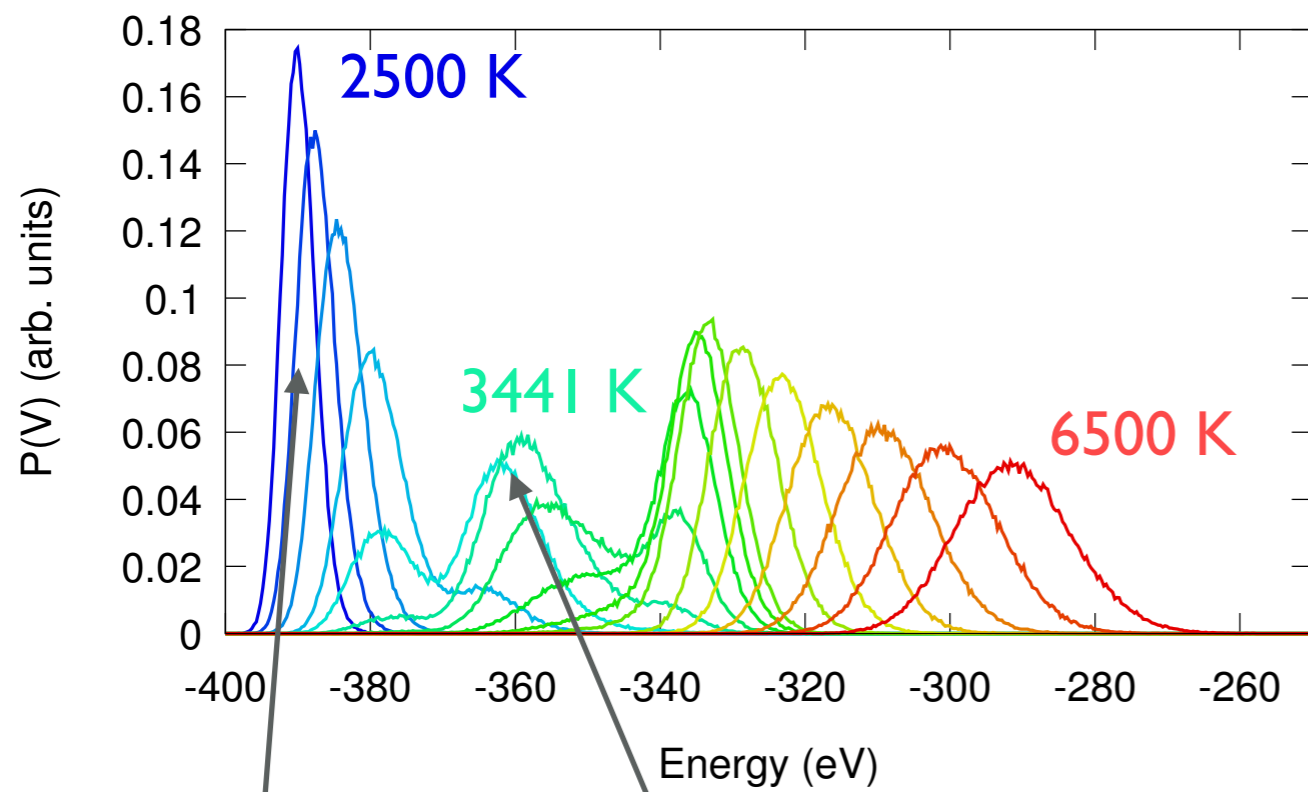


$\rho=0.15 \text{ g/cm}^3$ ,  $R=12.4 \text{ \AA}$

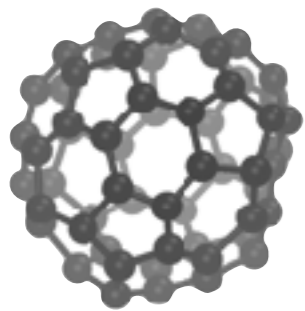


fullerenes

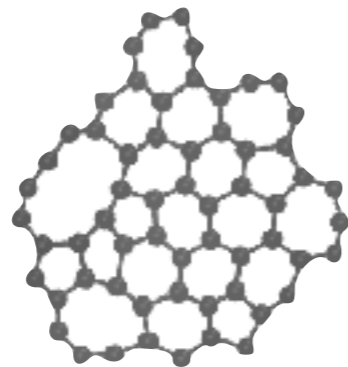
# C<sub>60</sub>: example of REMD simulation



$\rho=0.15 \text{ g/cm}^3$ ,  $R=12.4 \text{ \AA}$

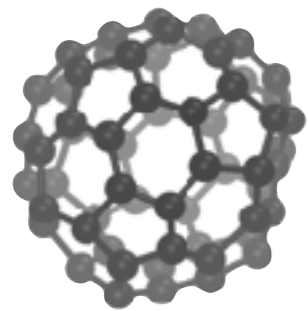
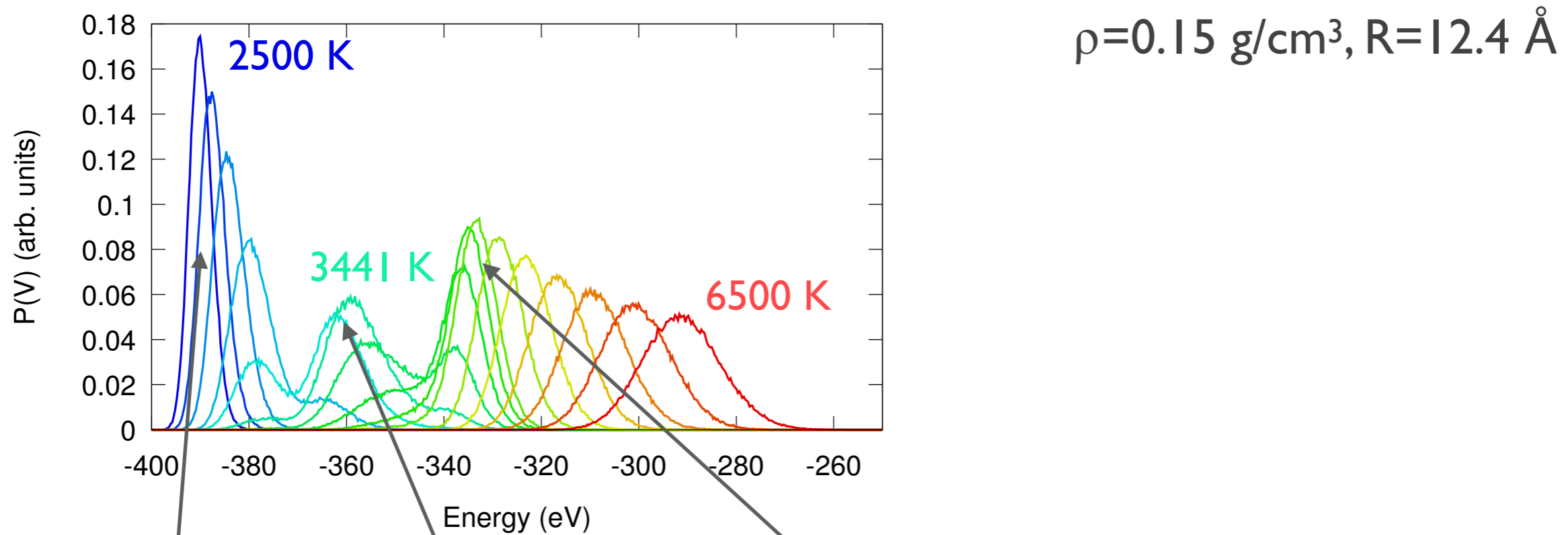


fullerenes

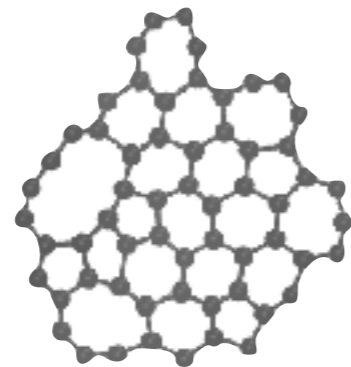


planar hexagonal

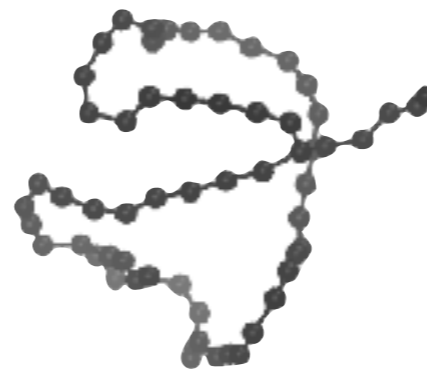
# C<sub>60</sub>: example of REMD simulation



fullerenes

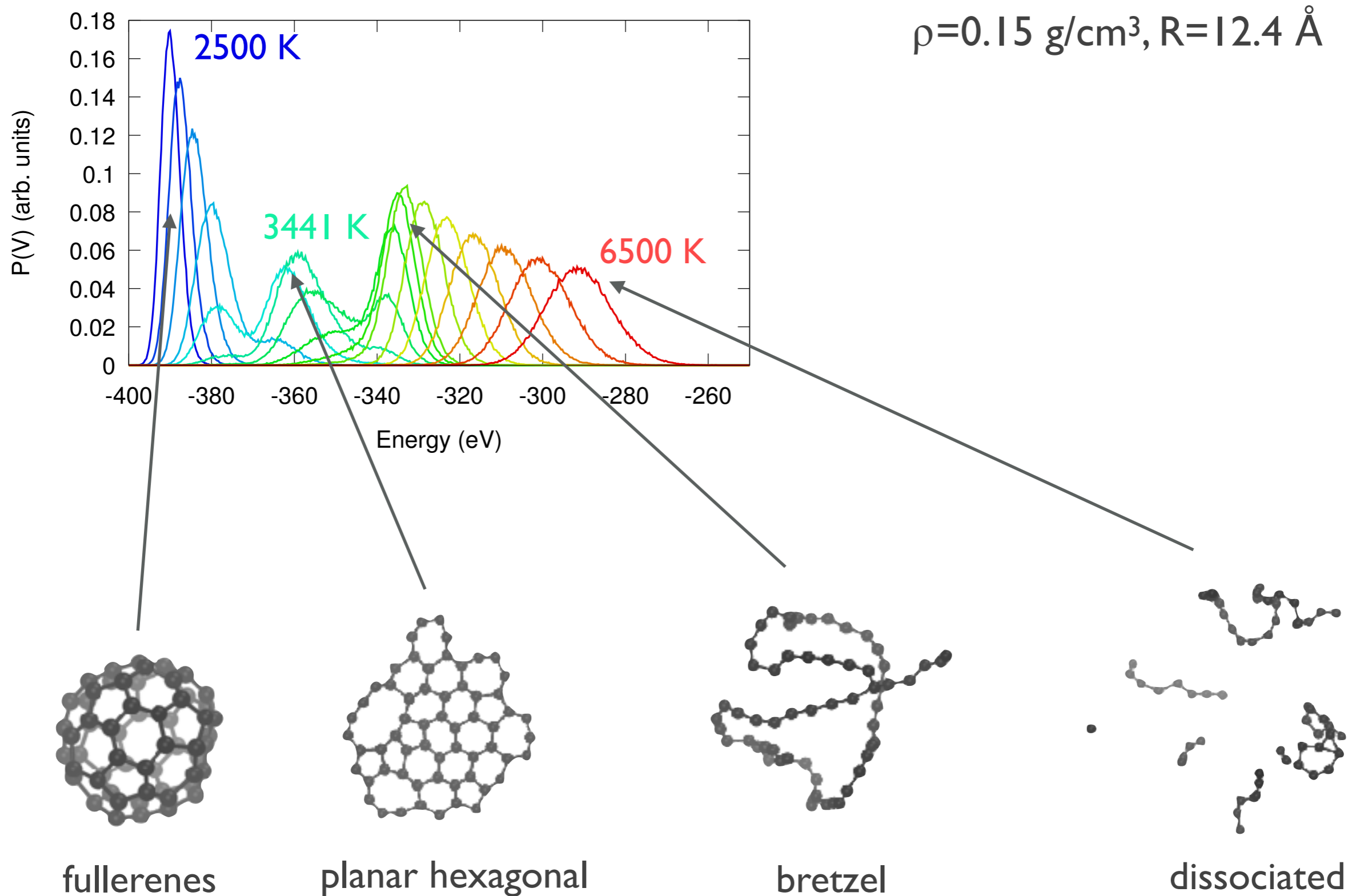


planar hexagonal



bretzel

# C<sub>60</sub>: example of REMD simulation





- Gyration tensor  $Q^{\alpha\beta} = \frac{1}{N} \sum_i \delta r_i^\alpha \delta r_i^\beta$        $\delta \mathbf{r}_i = \mathbf{r}_i - \mathbf{r}_g$

$$R_g^2 = \frac{1}{N} \sum_i \delta \mathbf{r}_i^2 = \text{Tr} \mathbf{Q} \quad \text{squared radius of gyration: spatial extension of the structure}$$

$$\mathbf{D} = \mathbf{Q} - \text{Tr} \mathbf{Q} \mathbf{I}$$

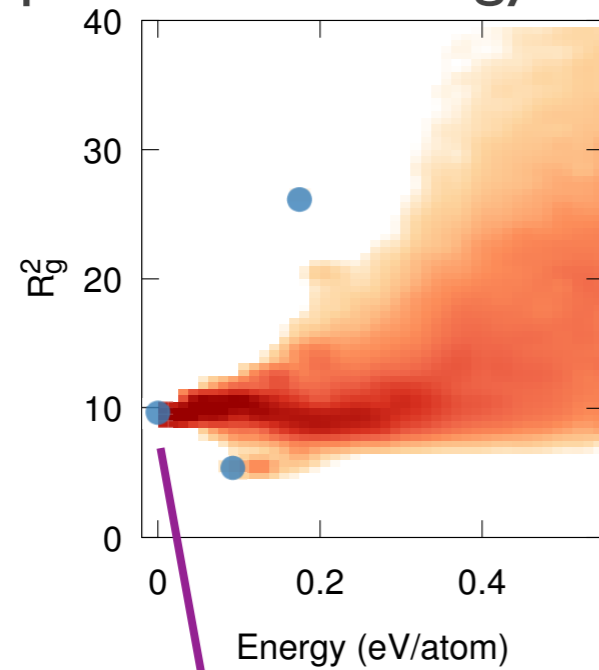
$$A_3 = \frac{3}{2} \frac{\text{Tr} (\mathbf{D}^2)}{(\text{Tr} \mathbf{Q})^2} \quad \text{asphericity: } A_3=0 \text{ for a sphere, } A_3=1 \text{ for a linear chain}$$

$$S = 27 \frac{\text{Det} (\mathbf{D})}{(\text{Tr} \mathbf{Q})^3} \quad \text{prolateness: } S=-0.25 \text{ for a plane, } S=2 \text{ for a linear chain}$$

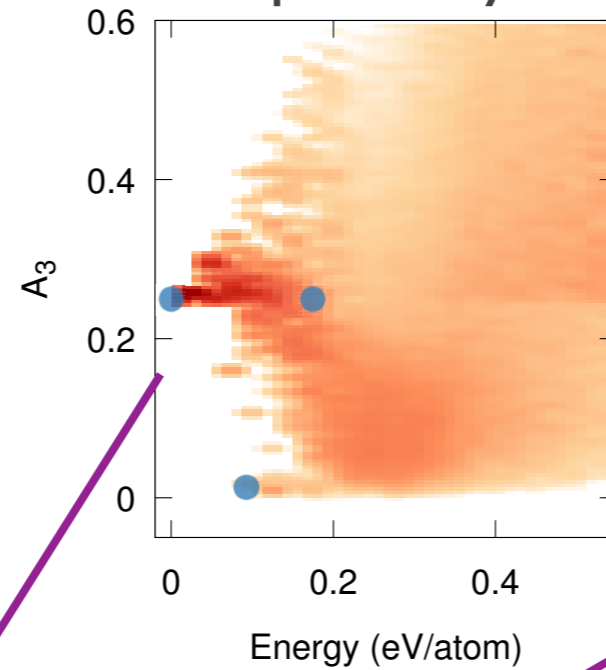
- Hybridization state: purely geometrical definition from the number of neighbors and the angles

# Analysis of the quenched structures: $C_{24}$

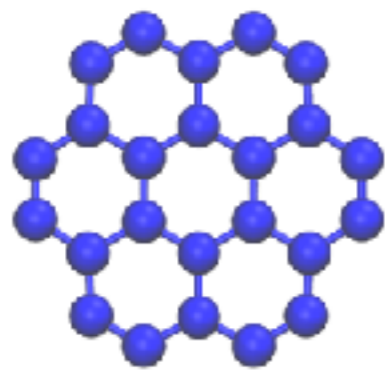
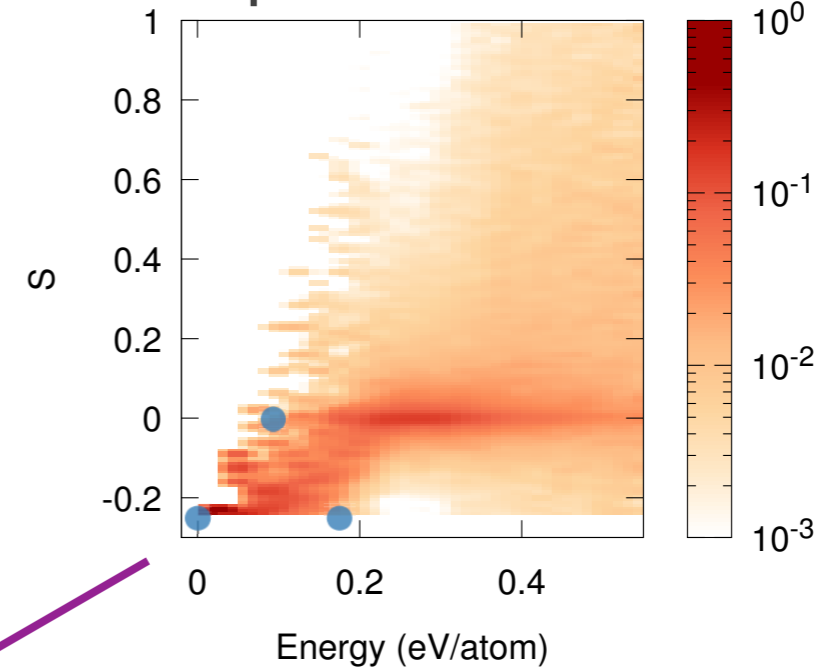
squared radius of gyration



asphericity



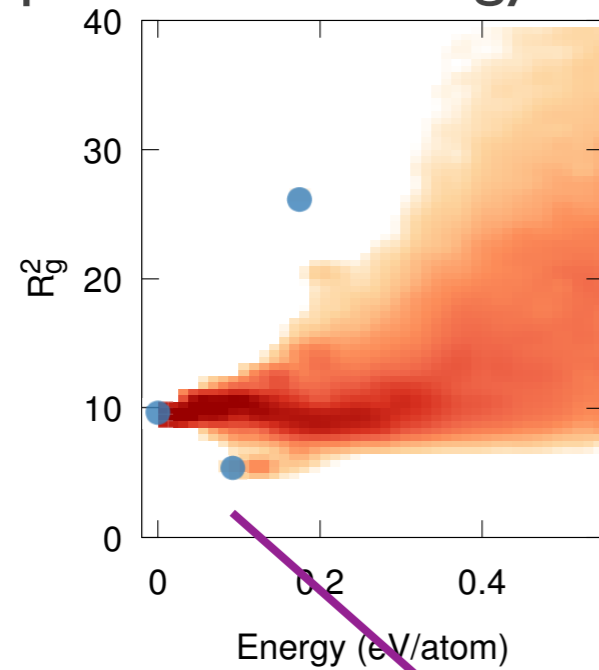
prolateness



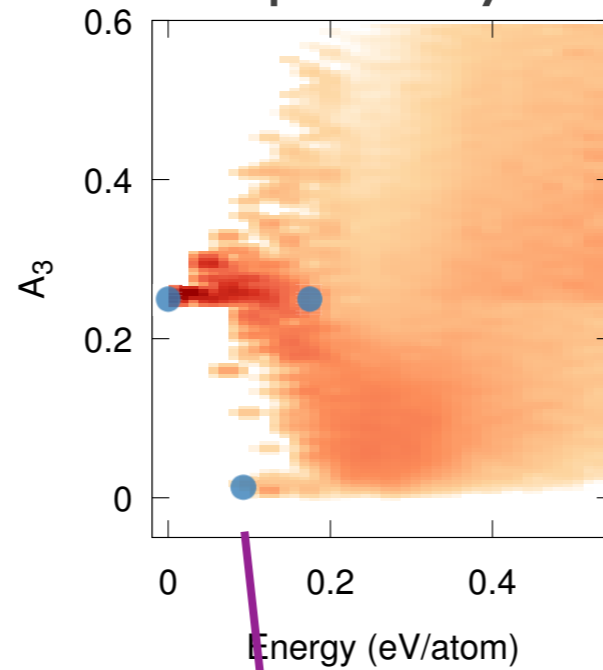
dehydrocoronene

# Analysis of the quenched structure: $C_{24}$

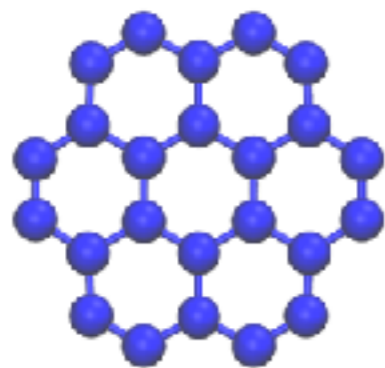
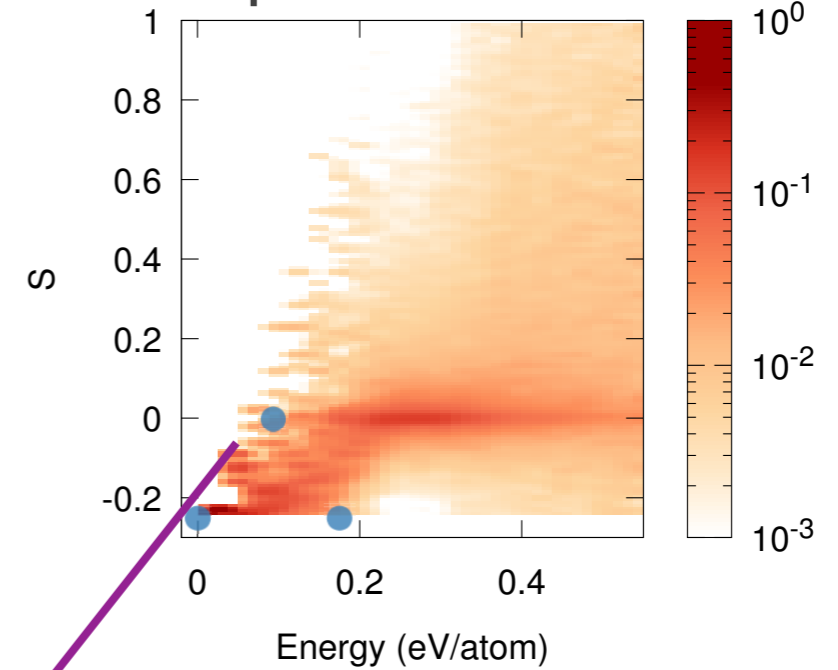
squared radius of gyration



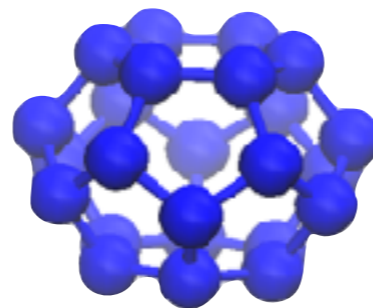
asphericity



prolateness



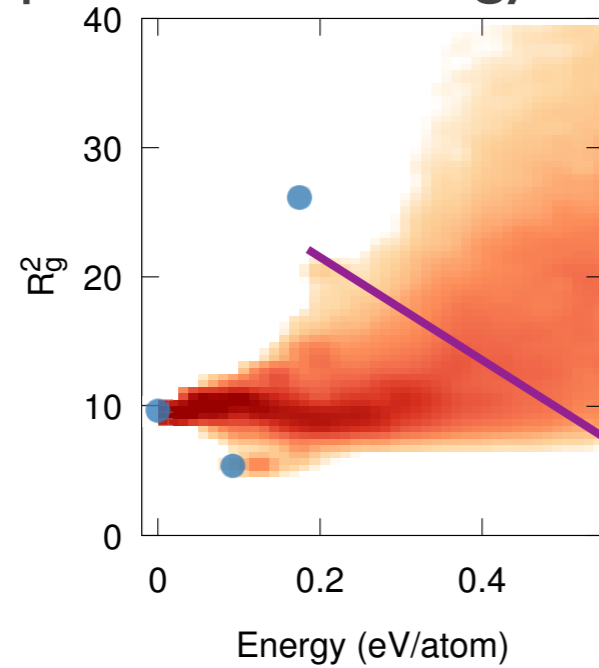
dehydrocoronene



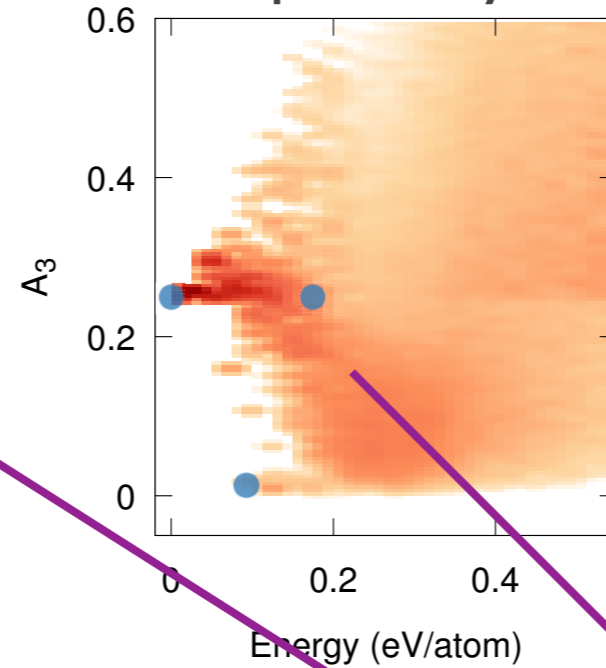
fullerene

# Analysis of the quenched structure: $C_{24}$

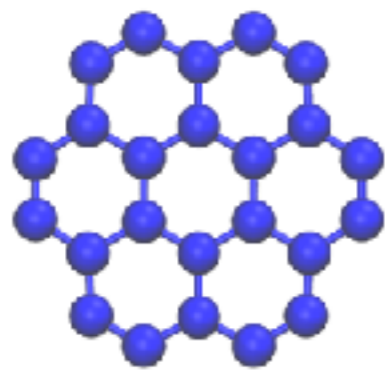
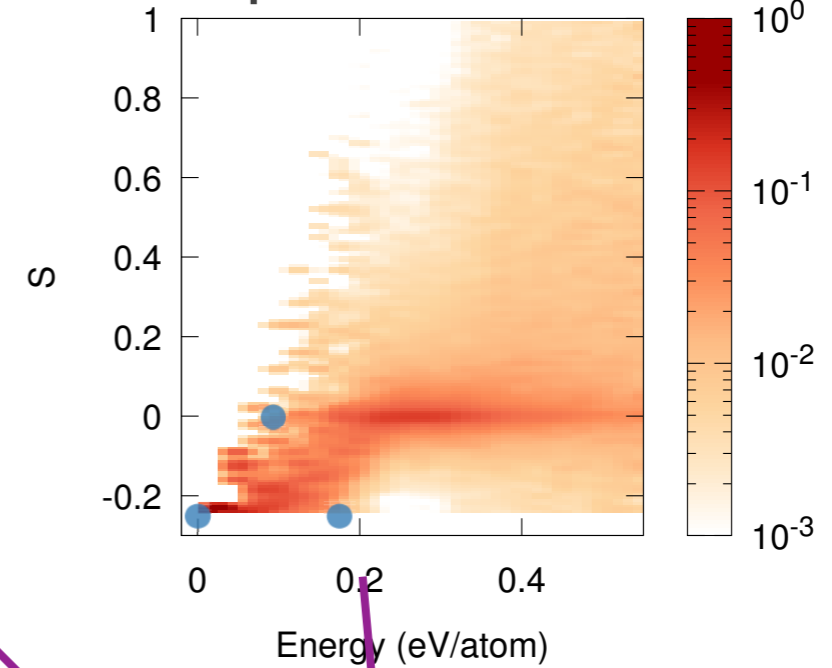
squared radius of gyration



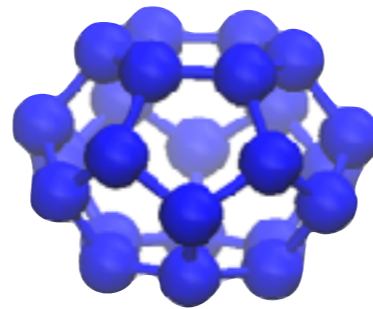
asphericity



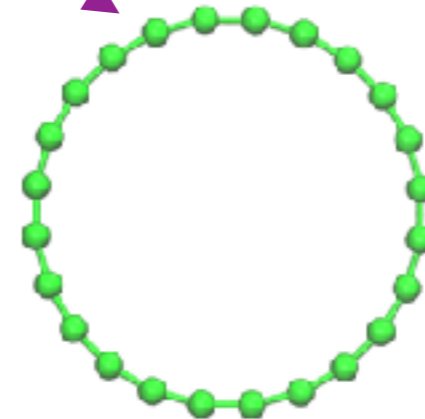
prolateness



dehydrocoronene



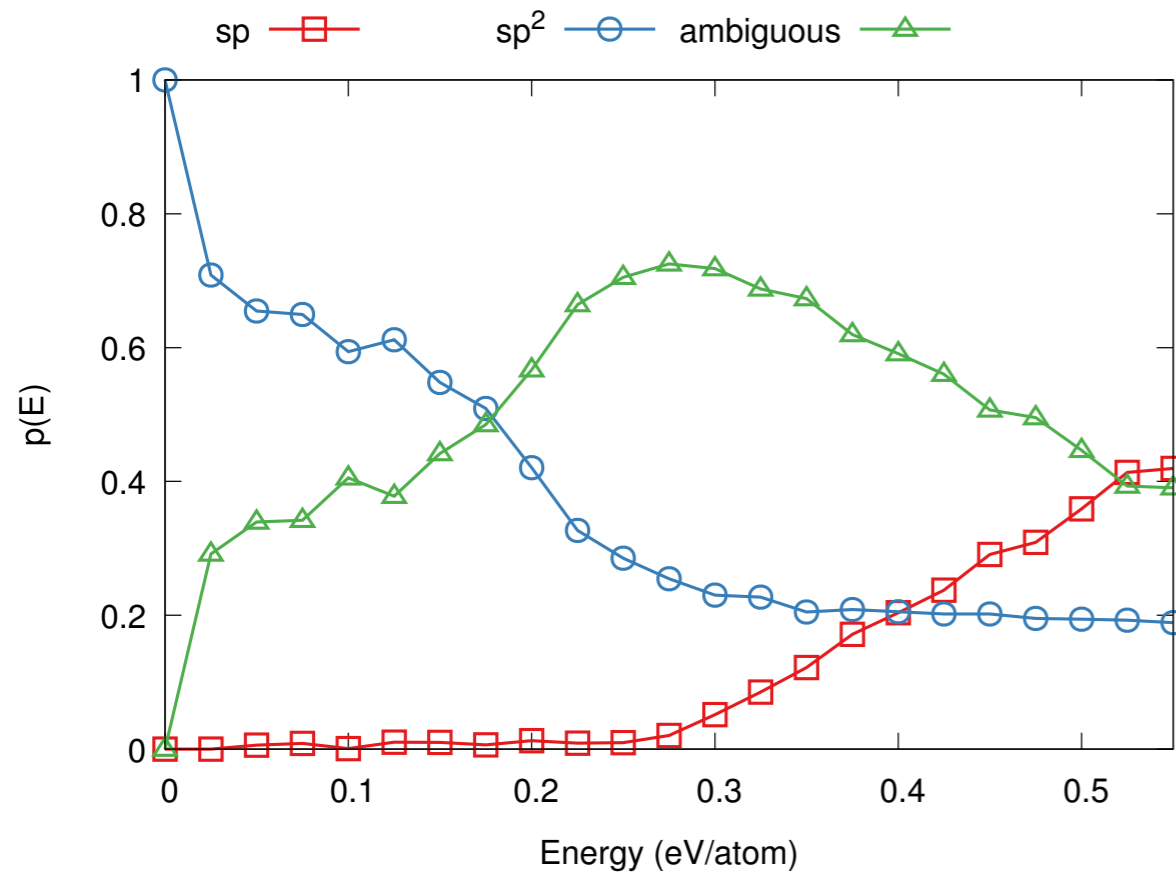
fullerene



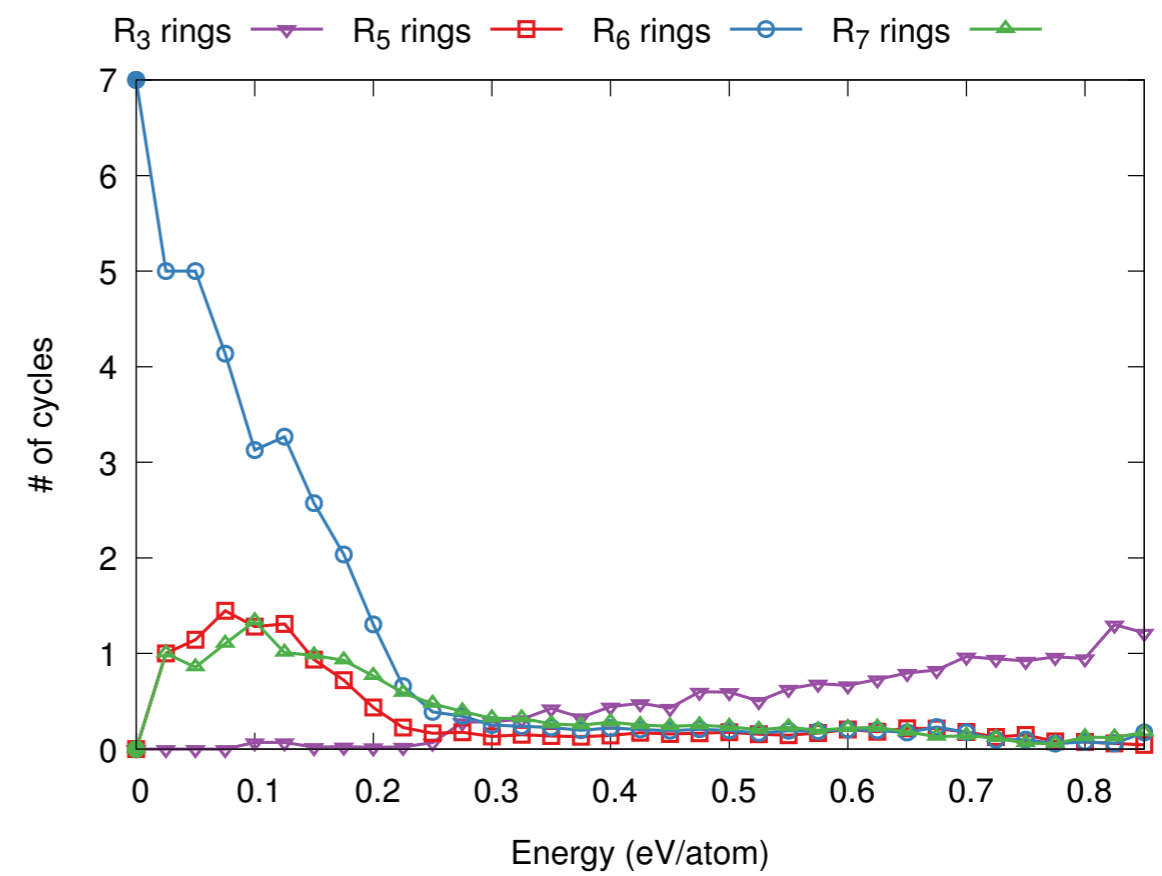
ring

# Analysis of the quenched structure: $C_{24}$

## hybridization state

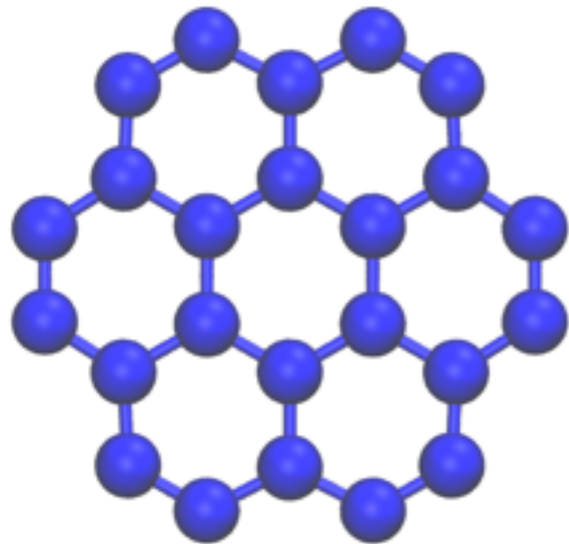


## # of cycles

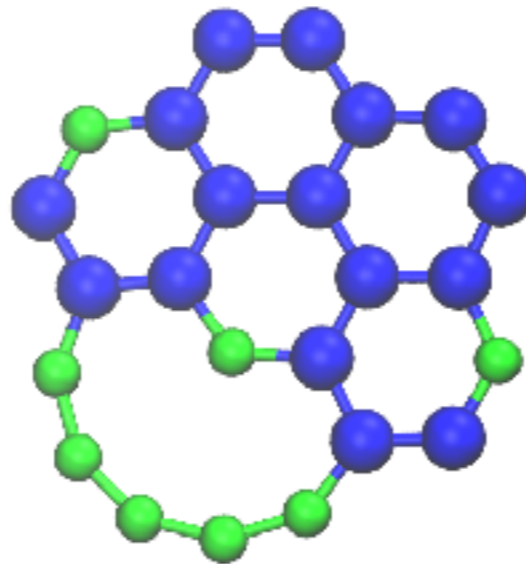


# Analysis of the quenched structures: $C_{24}$

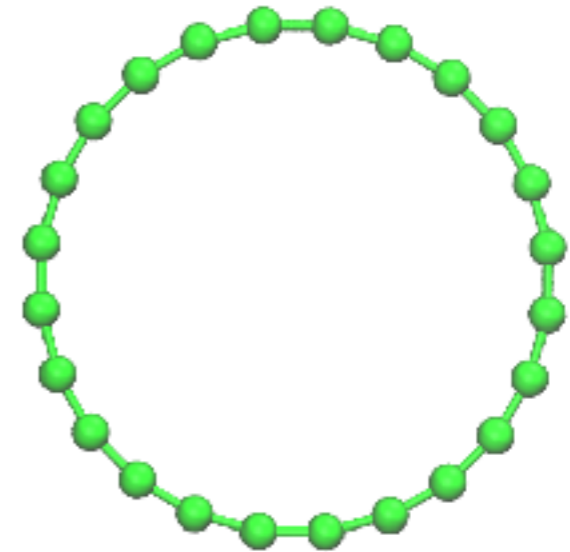
$E = 0$



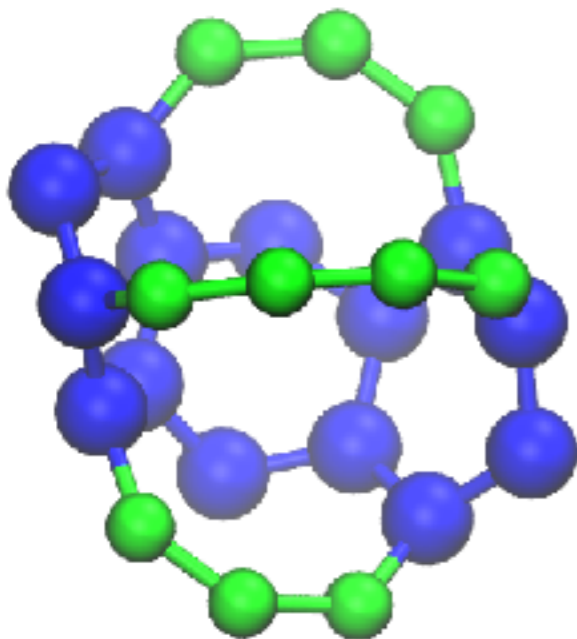
$E = 0.06$  eV/atoms



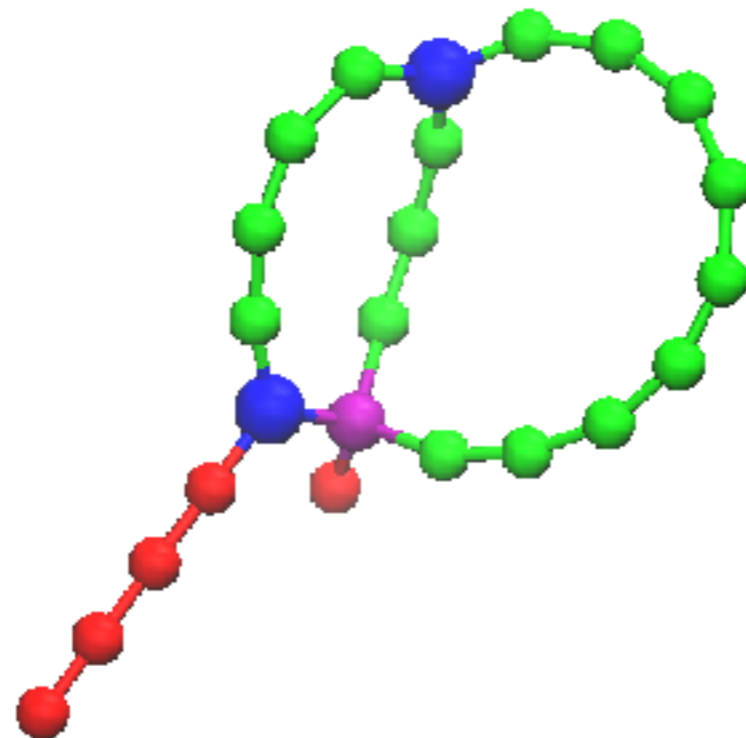
$E = 0.17$  eV/atoms



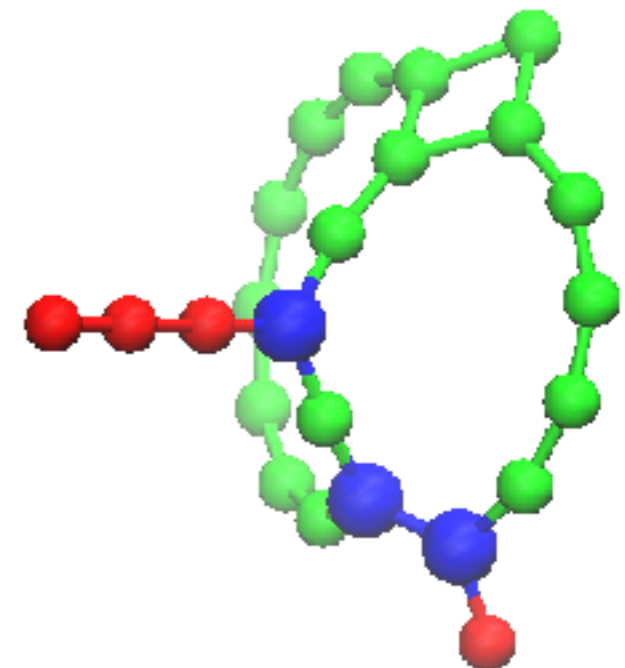
$E = 0.18$  eV/atoms



$E = 0.48$  eV/atoms

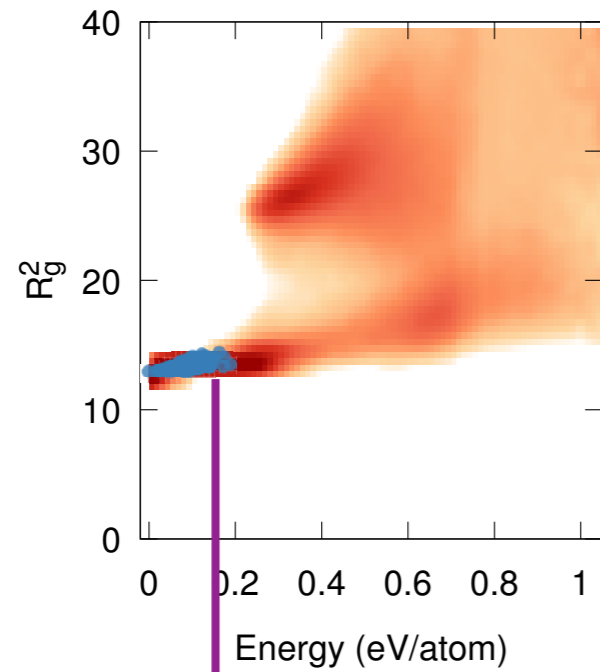


$E = 0.48$  eV/atoms

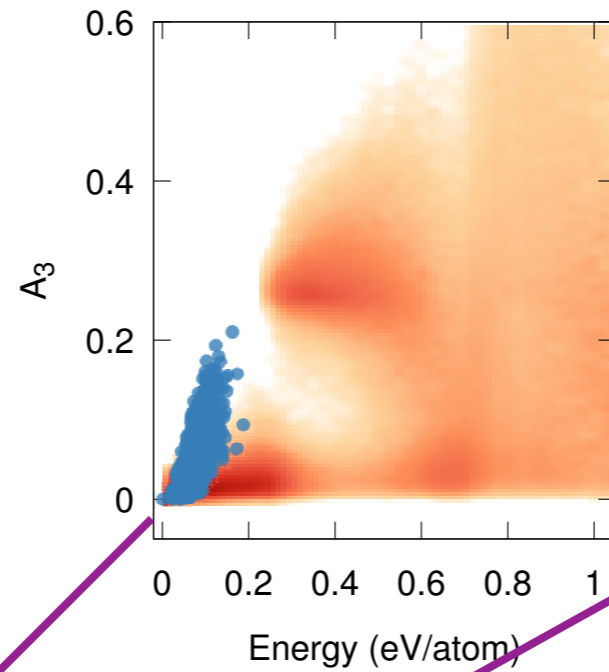


# Analysis of the quenched structure: $C_{60}$

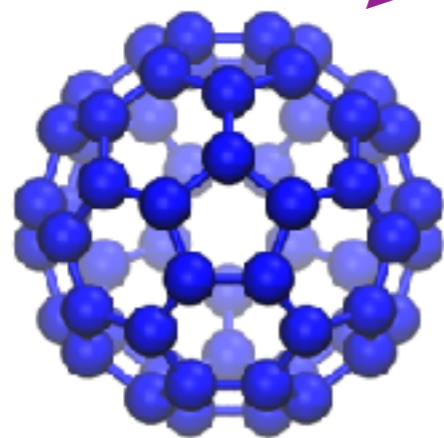
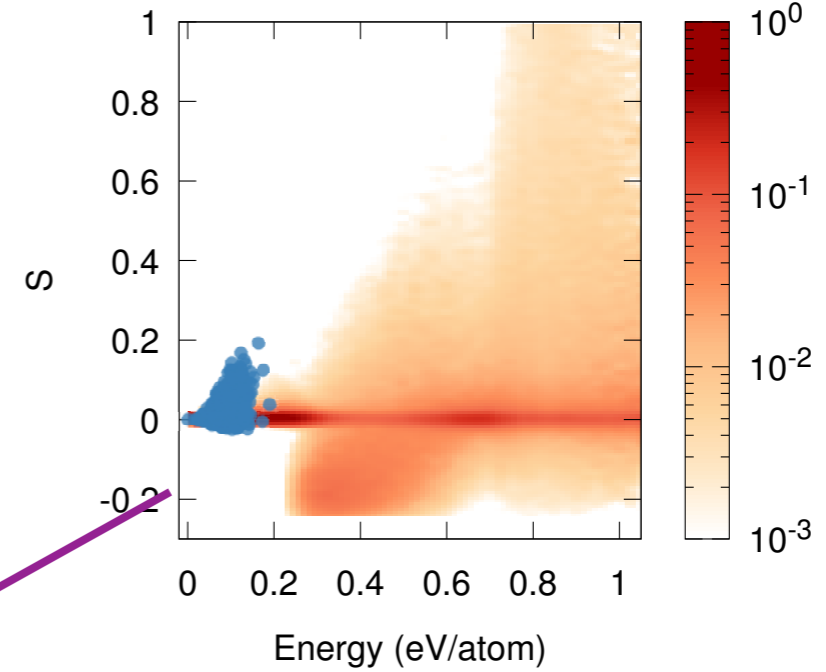
squared radius of gyration



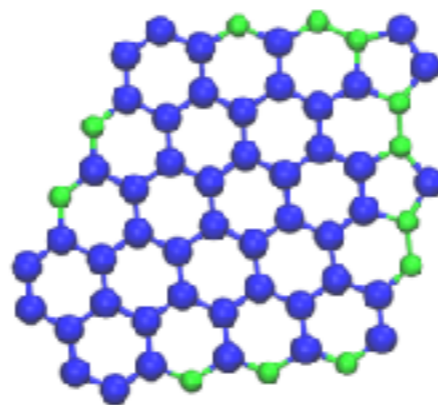
asphericity



prolateness



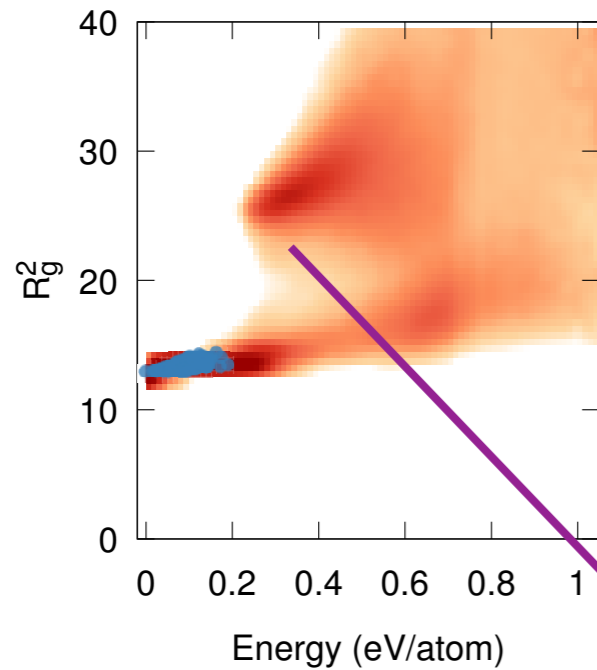
Fullerene isomers (I812)



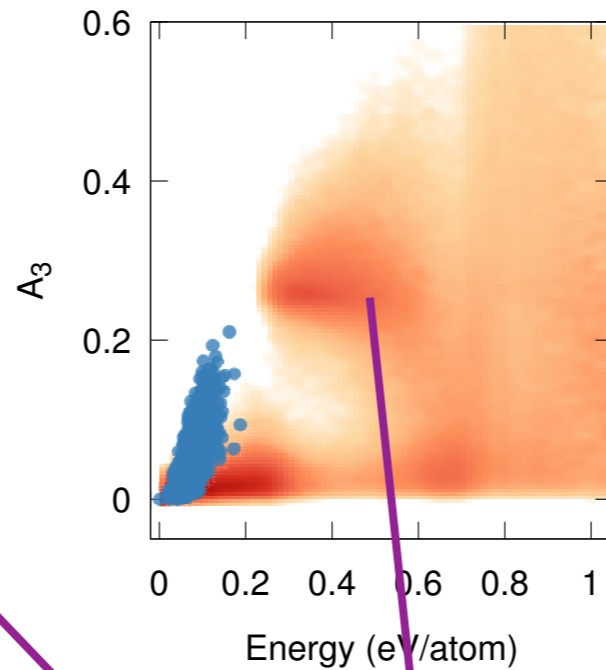
planar hexagonal

# Analysis of the quenched structure: $C_{60}$

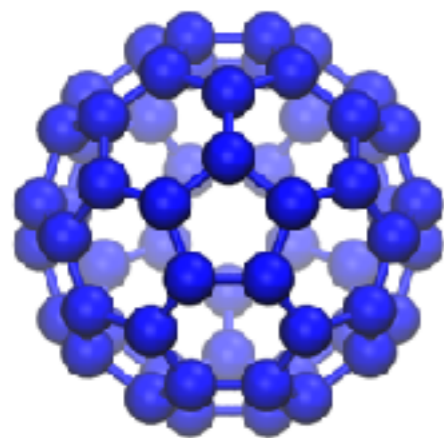
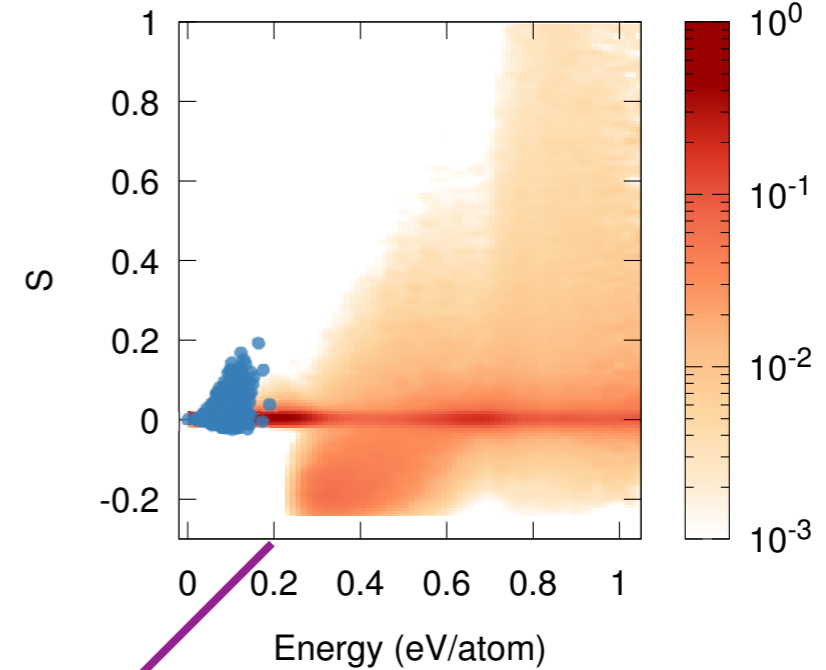
squared radius of gyration



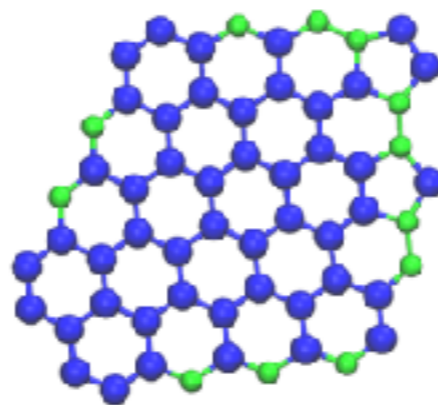
asphericity



prolateness



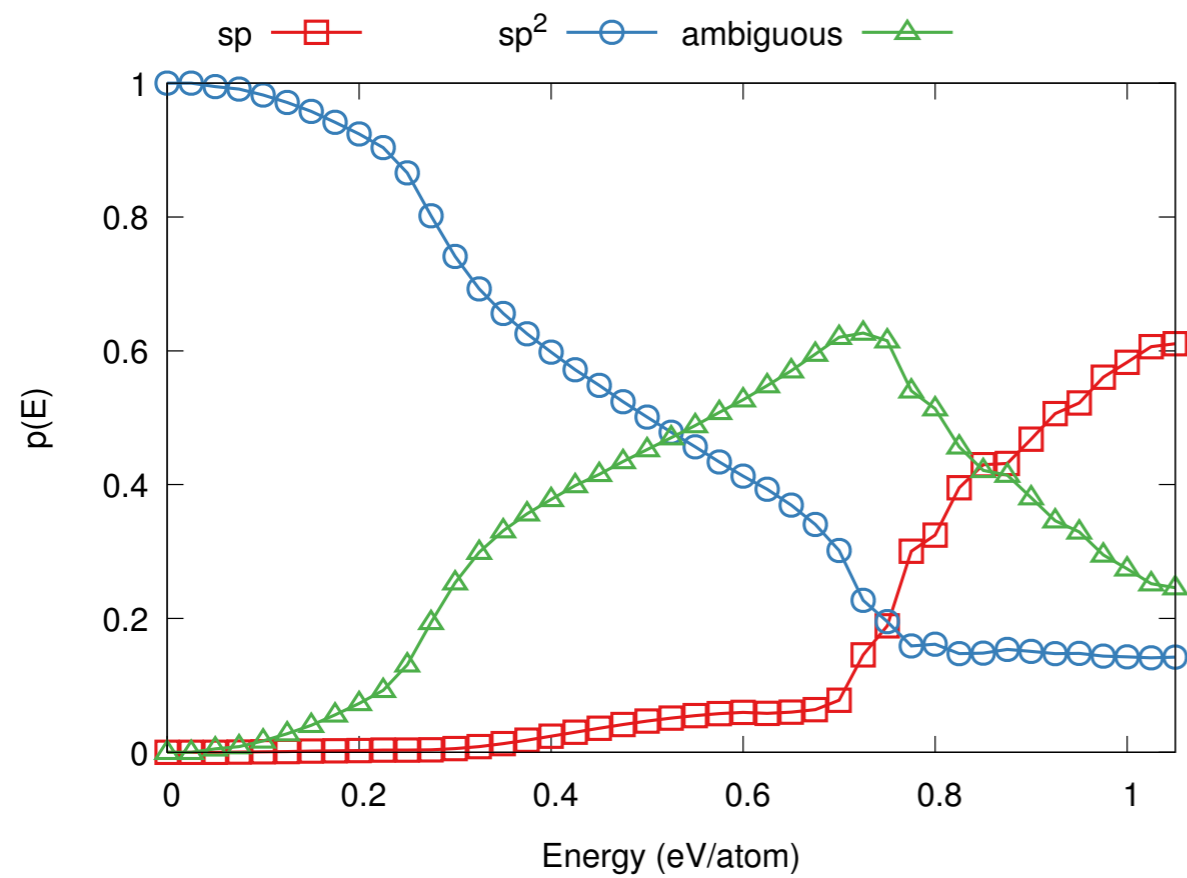
Fullerene isomers (1812)



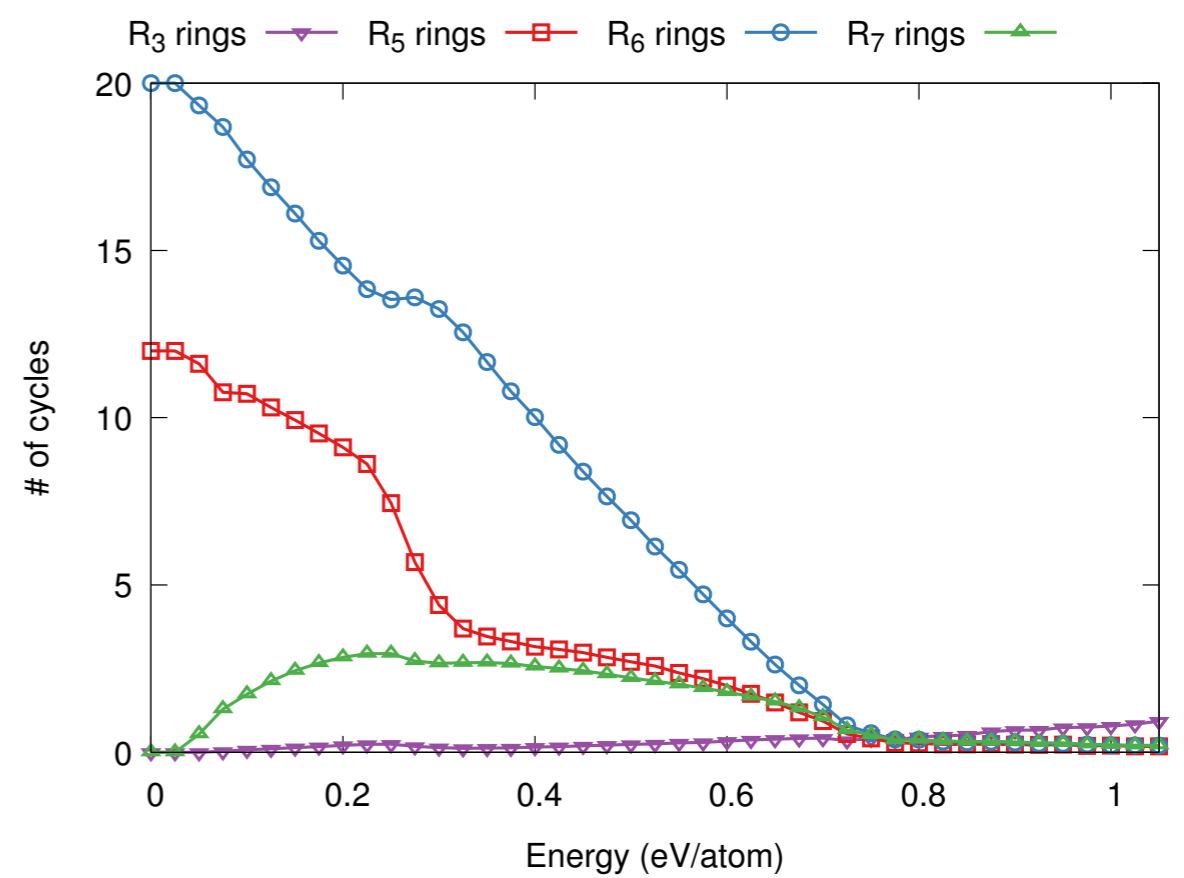
planar hexagonal



hybridization state

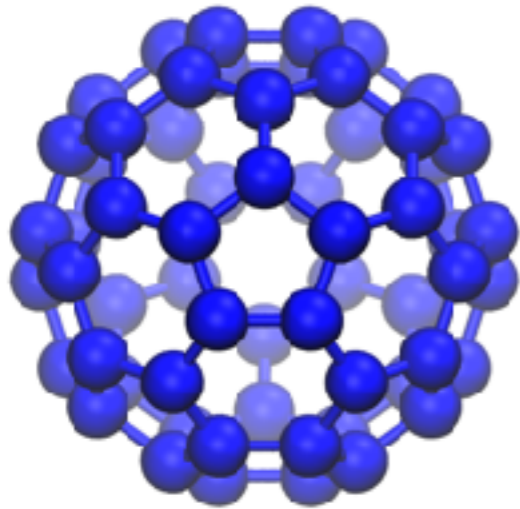


# of cycles

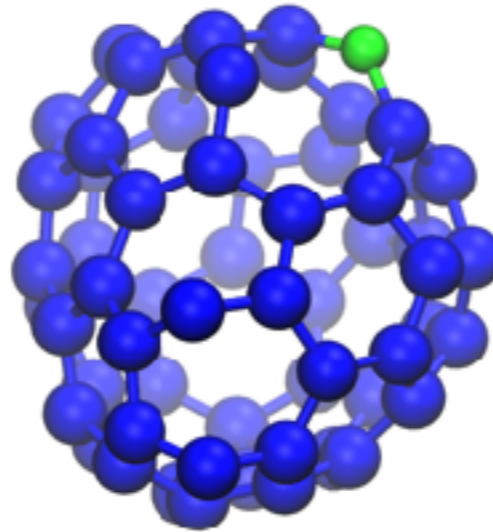


# Analysis of the quenched structures: $C_{60}$

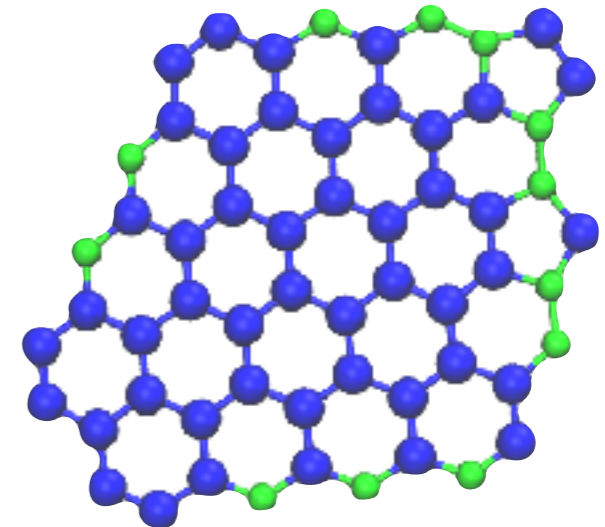
$E = 0$



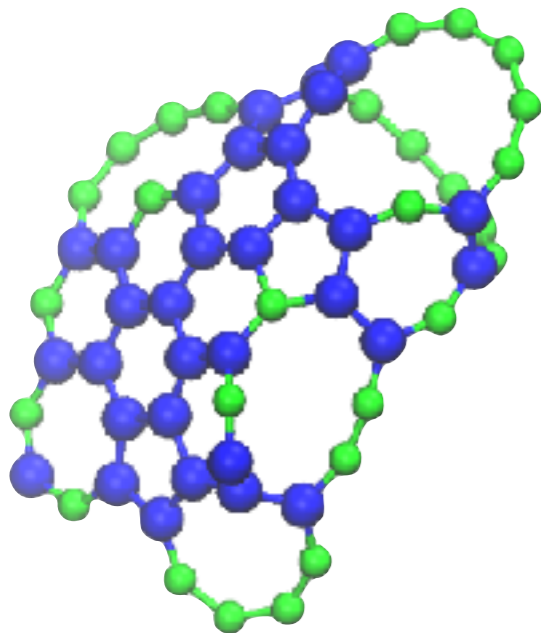
$E = 0.12$  eV/atoms



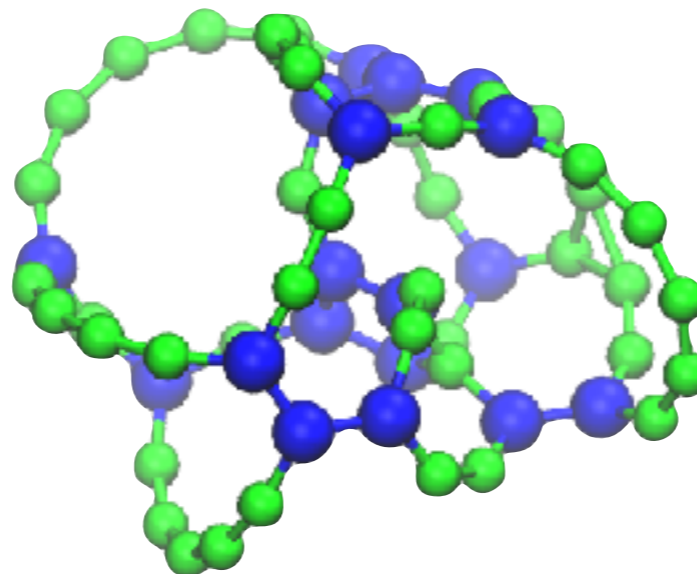
$E = 0.24$  eV/atoms



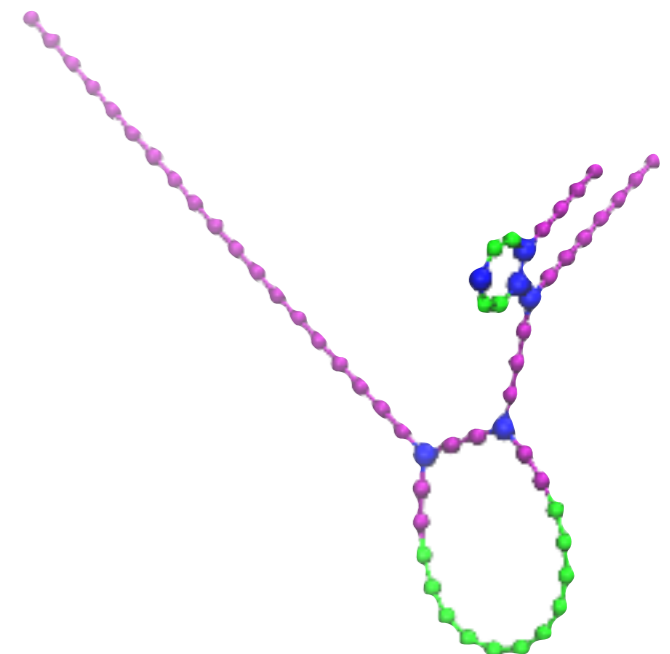
$E = 0.48$  eV/atoms



$E = 0.72$  eV/atoms



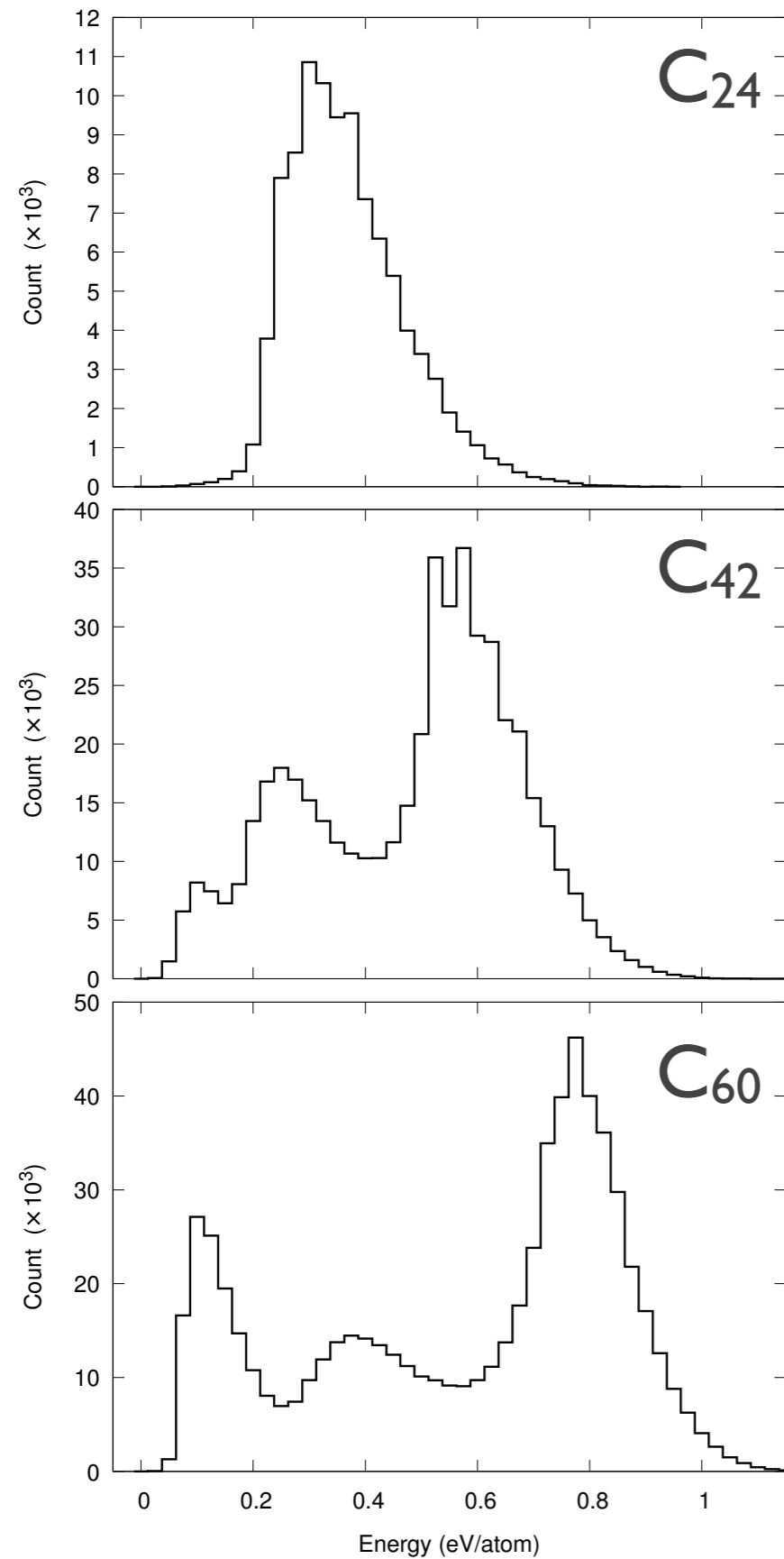
$E = 0.88$  eV/atoms



- LAMMPS is a power MD tool for simulate the structuration of carbon clusters
- The current implementation of (AI)REBO in LAMMPS is bug free
- AIREBO is not a derivable potential
- Some parameters in REBO need to be changed (this can be easily fixed)

THANKS FOR YOUR ATTENTION

# Energy distribution of quenched structures



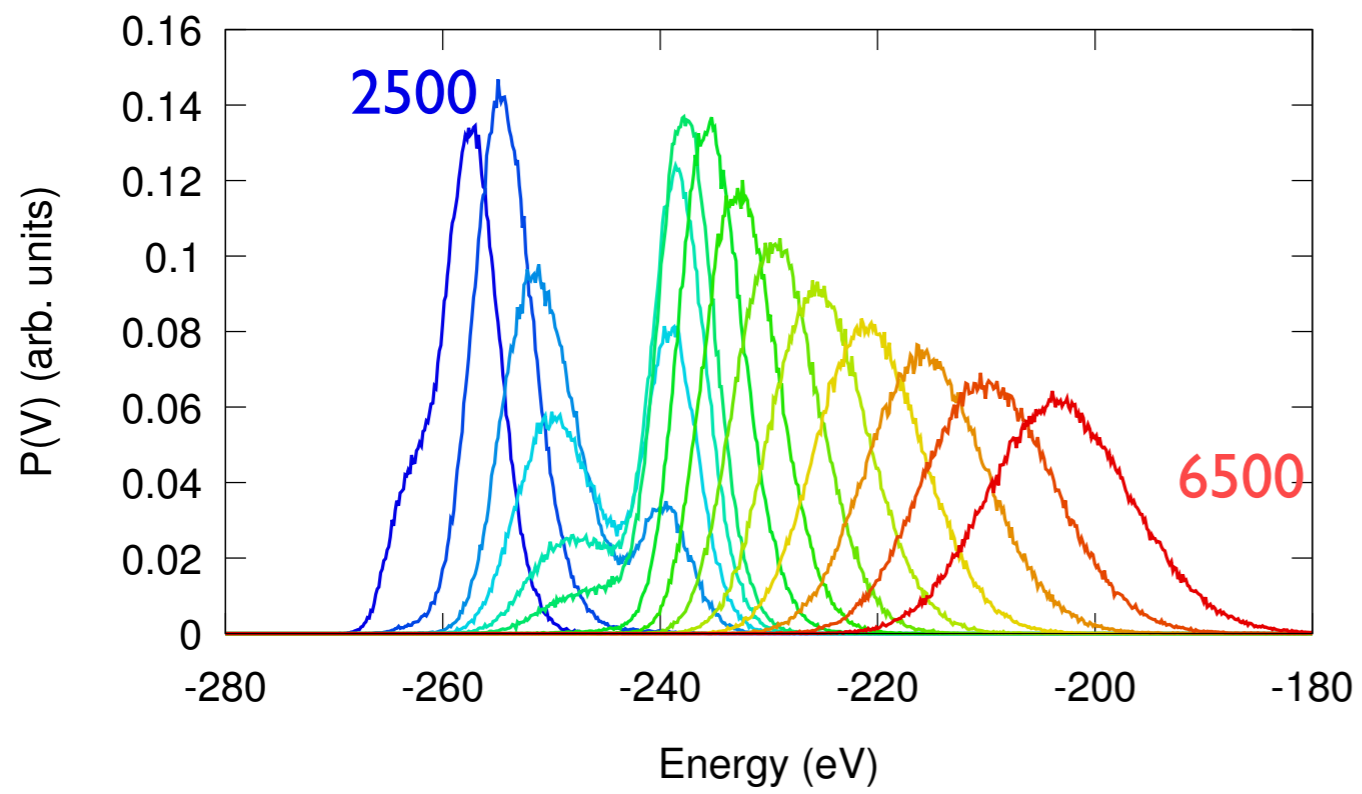
- Hybridization state: purely geometrical definition from the number of neighbors and the angles

$$\text{sp: } \begin{cases} N(i) = 1 \text{ or } 2, \\ \theta_k > 170^\circ \forall k. \end{cases}$$

$$\text{sp}^2: \begin{cases} N(i) = 2 \text{ or } 3, \\ 100^\circ < \theta_k < 125^\circ \forall k, \\ \text{Var}(\theta_k) < 12^\circ. \end{cases}$$

$$\text{sp}^3: \begin{cases} N(i) = 4, \\ 100^\circ < \theta_k < 120^\circ \forall k, \\ \text{Var}(\theta_k) < 12^\circ. \end{cases}$$

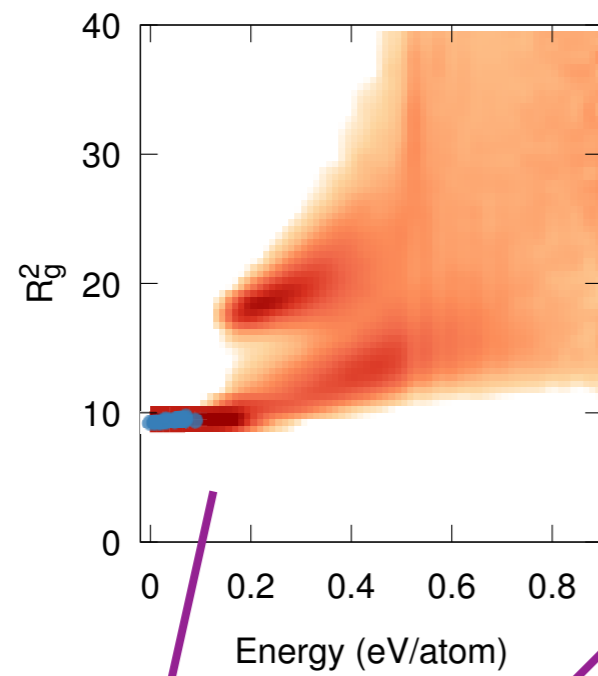
# C<sub>42</sub>: exemple of REMD simulation



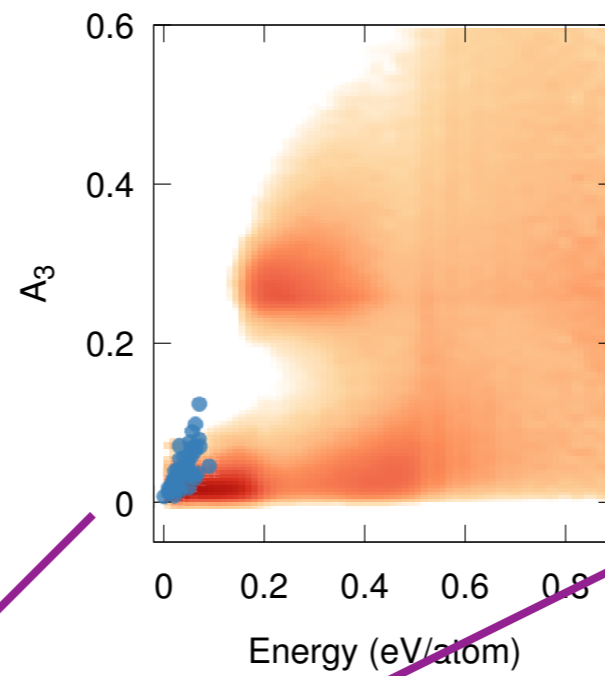
$\rho=0.15 \text{ g/cm}^3$ ,  $R=11 \text{ \AA}$

# Analysis of the quenched structure: $C_{42}$

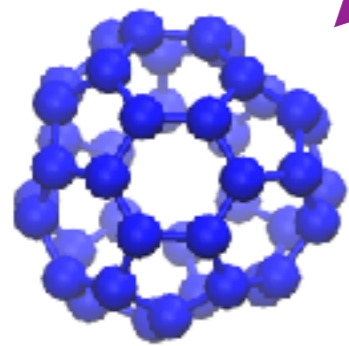
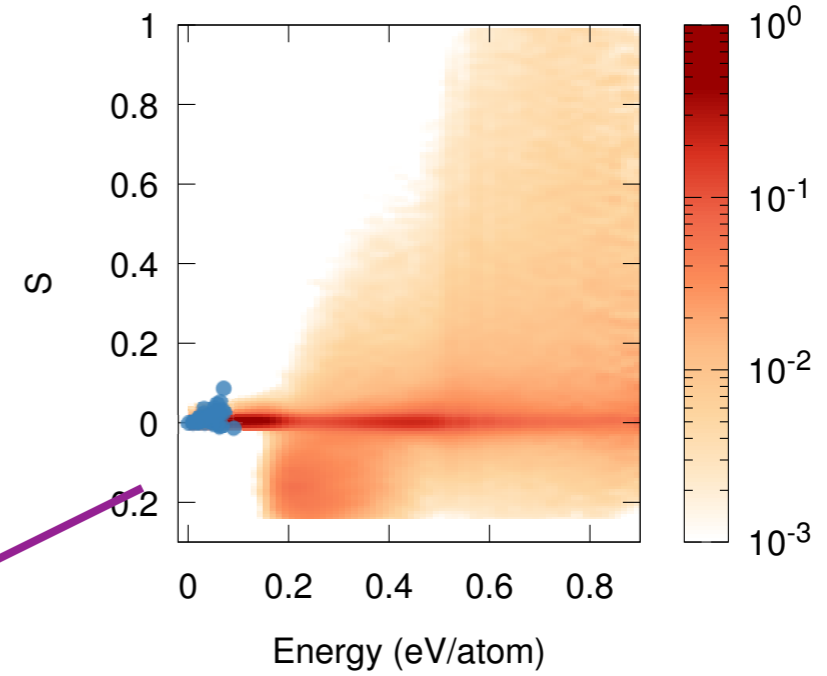
squared radius of gyration



asphericity



prolateness

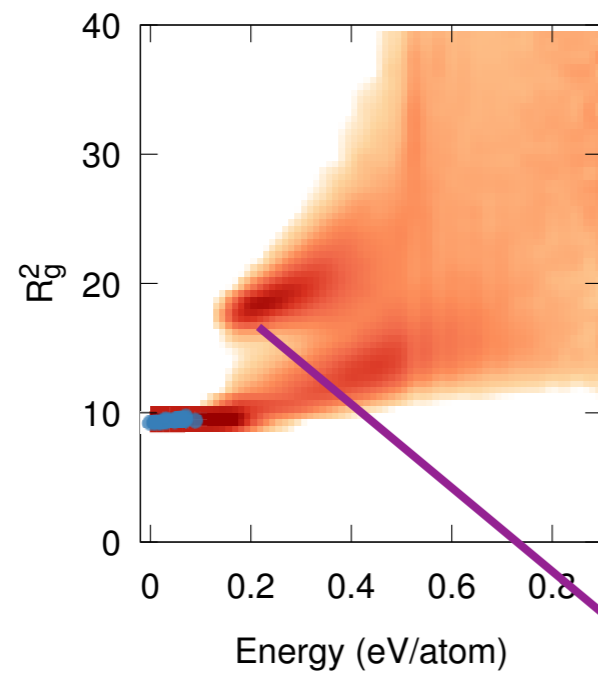


45 fullerene isomers

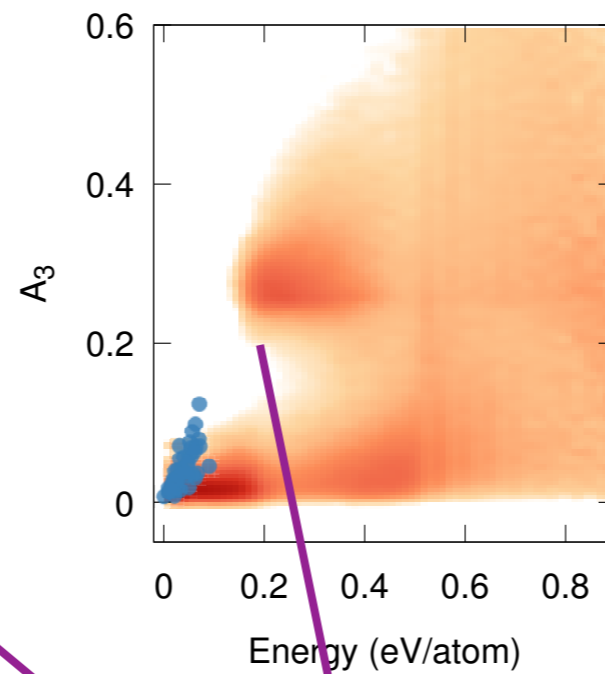


# Analysis of the quenched structure: $C_{42}$

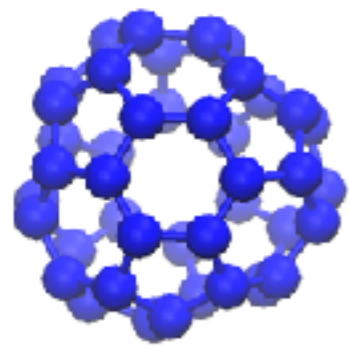
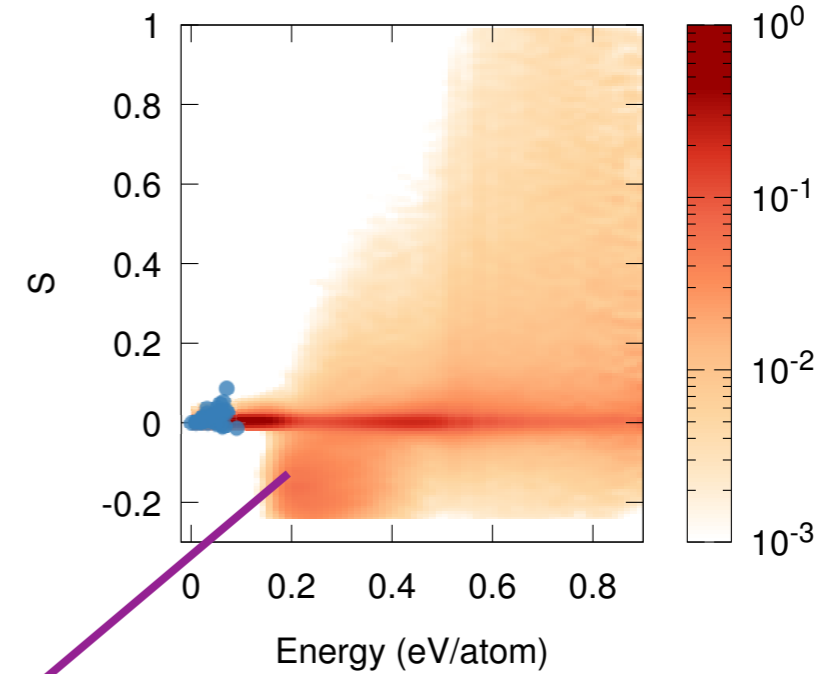
squared radius of gyration



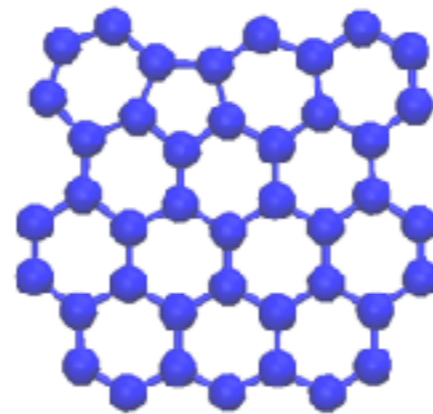
asphericity



prolateness



45 fullerene isomers



planar structures

# Analysis of the quenched structure: C<sub>42</sub>

